Off-fault damage and acoustic emission distributions during the evolution of structurally complex faults over series of stick-slip events

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Accepted 2014 February 24. Received 2014 February 19; in original form 2013 October 5

SUMMARY
Variations in fault structure, for example, surface roughness and deformation zone width, influence the location and dynamics of large earthquakes as well as the distribution of small seismic events. In nature, changes in fault roughness and seismicity characteristics can rarely be studied simultaneously, so that little is known about their interaction and evolution. Here, we investigate the connection between fault structure and near-fault distributions of seismic events over series of stick-slip cycles in the laboratory. We conducted a set of experiments on rough faults that developed from incipient fracture surfaces. We monitored stress and seismic activity which occurred in the form of acoustic emissions (AEs). We determined AE density distributions as a function of fault normal distance based on high-accuracy hypocentre locations during subsequent interslip periods. The characteristics of these distributions were closely connected to different structural units of the faults, that is, the fault core, off-fault and background damage zone. The core deformation zone was characterized by consistently high seismic activity, whereas the off-fault damage zone displayed a power-law decay of seismic activity with increasing distance from the fault core. The exponents of the power-law-distributed off-fault activity increased with successive stick-slip events so that later interslip periods showed a more rapid spatial decay of seismic activity from the fault. The increase in exponents was strongest during the first one to three interslip periods and reached approximately constant values thereafter. The relatively rapid spatial decay of AE events during later interslip periods is likely an expression of decreasing fault zone complexity and roughness. Our results indicate a close relationship between fault structure, stress and seismic off-fault activity. A more extensive mapping of seismic off-fault activity-decay has the potential to significantly advance the understanding of fault zone properties including variations in fault roughness and stress.

Key words: Microstructures; Seismicity and tectonics; Statistical seismology; Rheology and friction of fault zones; Dynamics and mechanics of faulting; Fractures and faults.

1 INTRODUCTION
The complexity of strain accumulation along tectonic plate boundaries, which are comprised of systems of faults, poses a challenge for the predictability of earthquakes. Earthquake rupture initiation and propagation is strongly influenced by the frictional properties and structure of faults. Faults are zones of high strain within the upper crust, consisting of a fault core surrounded by a zone of distributed damage (e.g. Caine et al. 1996; Ben-Zion & Sammis 2003). This damage zone consists of joints, cracks, pulverized rock and subsidiary faults over a wide range of length scales, and the embedded fault core contains a gouge layer, as well as anastomosing principal and secondary zones of slip localization (e.g. Chester & Logan 1986; Chester et al. 1993; Faulkner et al. 2003; Dot et al. 2006; Wibberley et al. 2008; Faulkner et al. 2010). The structure of fault zones varies along fault-strike and depends on both protolith composition and rock-fluid interactions (e.g. Schulz & Evans 2000; Faulkner et al. 2003, 2008; Smith et al. 2013). Current models of fault zone structure suggest that faults are heterogeneous but become less complex with increasing displacements so that most of the slip on mature faults occurs within zones of highly localized strain (e.g. Chester et al. 1993; Chester & Chester 1998; Ben-Zion & Sammis 2003). This is supported by geological observations of large off-set fault zones in Southern California (e.g. Chester & Chester 1998; Rockwell & Ben-Zion 2007). Fault evolution has additionally been

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documented by decreasing numbers of fault stepovers (e.g. Wesnousky 1988), and decreasing geometric disorder of fault surface traces (Wechslers et al. 2010) with increasing cumulative displacements. These studies generally indicate a continuous evolution towards less complexity even after large amounts of slip (1–300 km) have been accumulated. This is in agreement with results from seismicity inferred fault smoothing which appears to be active at displacements of up to ∼300 km (Powers & Jordan 2010). However, other studies which examined roughness of exhumed fault surfaces suggested that large off-set faults remain in a state of constant complexity (Sagy et al. 2007; Candela et al. 2012), possibly due to decreasing rates of abrasional smoothing caused by gouge lubrication (Brodsky et al. 2011) or rupture related fault re-roughening (Bhat et al. 2007; Candela et al. 2011a,b; Klinger et al. 2010). The apparent discrepancies in studies on fault roughness reduction as function of fault maturity raise questions about the uniformity of fault evolution. Fault roughness reduction may be scale-dependent, or a transient process that is only active on relatively young faults.

A better documentation of fault evolution is vital for the understanding of many upper crustal processes. A reduction in fault roughness, for example, influences the characteristics of strain release during fault slip including slip distributions, stress drops and off-fault stresses (Power & Tullis 1995; Dieterich & Smith 2009; Candela et al. 2011a,b; Dunham et al. 2011). Moreover, the degree of slip localization and roughness reduction of evolving fault zones govern many fault processes related to fault-hydrology, fault-zone growth, earthquake-rupture dynamics and the near-fault distribution of seismic events (e.g. Ben-Zion & Sammis 2003; Wibberley et al. 2008; Faulkner et al. 2010; Powers & Jordan 2010). Similarly, the geometry of systems of faults controls local earthquake interactions and seismicity clustering. Models that include these fault-system-induced interactions can produce seismicity characteristics similar to regional observations and replicate observed statistical relations of natural seismicity, including aftershock clustering (e.g. Ward 2000; Rundle et al. 2004; Dieterich & Richards-Dinger 2010). Thus, a more detailed understanding of fault evolution and its controls on seismic event distribution is essential, not least for seismic hazard assessment.

Geologic observations of fault-zone structure are commonly limited to inactive, exhumed fault branches, so that an investigation of fault structure, fault evolution and associated variations in seismicity distributions is not straightforward. To overcome these limitations, we study fault evolution and seismic event distributions on complex fault zones in laboratory experiments under upper crustal stress-conditions. We present results from series of stick-slip experiments on laboratory-created fault zones during which we document stress, strain, and seismic activity as well as post-experimental fault structures. We previously tested the connection between roughness and seismicity-density distributions on planar surfaces with predefined roughness showing that the off-fault activity can be described by a power law which is controlled by fault roughness and normal stress (Goebel et al. 2014). The observed power-law distributions are in agreement with a theoretical study on the effects of fractal roughness on off-fault seismicity distributions (Dieterich & Smith 2009). We extend the previous experiments through the creation of series of stick-slip events on structurally complex fault zones that developed from incipient, natural fracture surfaces. The current study is divided into three parts: Initially, we compare fault zone structure observed in computer tomography (CT) scans, photographic images and thin sections with acoustic emission (AE) density distributions. We then investigate changes in AE density distributions with successive stick-slip events as possible indicator for progressive fault smoothing. Finally, we examine the connection between variations in normal stress and seismic off-fault activity distributions.

### 2 DATA AND METHOD

We show results from four frictional sliding experiments (WG04, WG05, WG07 and WG08) on Westerly granite surfaces, loaded under triaxial compression. Prior to loading, the rock samples were prepared with saw-cut notches at 30° angles to the loading axis to concentrate deformation towards the centre of the samples (see Fig. S1 and Goebel et al. 2012, for schematic representations of sample geometry and loading conditions). Initially, we fractured the intact part between the notches. We then increased the confining pressure to lock the faults and loaded the samples axially resulting in series of stick-slip events (see supporting information for more details). The current study focuses on results from the stick-slip sliding phase of these experiments. This phase was generally conducted at a constant axial displacement rate (20 μm s⁻¹) and constant confining pressure (Pc = 150 MPa). Changes in differential stress were determined from force measurements of an external load cell. Fault normal stresses were computed under consideration of changing fault geometries, that is, we corrected for different notch depths and changes in effective fault surface area due to slip (Scott et al. 1994; Temble et al. 2010). A summary of loading conditions, sample geometry, and stresses are found in Table 1.

The deformation along the laboratory-created fault zones was connected to high AE activity. To document the AE activity, we employed a high-speed (10 MHz sampling frequency) and high-accuracy (16 bits amplitude resolution) data acquisition system (see Stanchits et al. 2006, for details). AE events were recorded using a miniature seismic-array, consisting of 16 piezo-electric transducers. AE event locations were determined from traveltine inversions of automatically picked first arrival times. The location-uncertainty of AE hypocentres was estimated at 1–4 mm, depending on the proximity of an event to the limits of seismic array coverage. The total number of located AEs varied between ∼30 000 to ∼100 000 for the different experiments (see Goebel et al. 2013a).

The analysis of fault-normal AE distributions within this study largely follows Goebel et al. (2014). Initially, we projected the recorded AE hypocentre locations into the corresponding, best-fitting fault coordinate systems. The spatial decay of AE events relative to the fault was determined from linear density estimates (e.g. Silverman 1986) analogous to previous studies of natural seismicity (Hauksson 2010; Powers & Jordan 2010). Fault-normal AE densities were computed by sampling a constant number (N) of

<table>
<thead>
<tr>
<th>Experiment</th>
<th>lₜₙ</th>
<th>σₐₐₑ</th>
<th>Uₑ</th>
<th>σₐ</th>
<th>τ</th>
<th>(MPa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>WG04</td>
<td>5.0 ± 0.15</td>
<td>365 ± 6.35</td>
<td>3.0 ± 0.003</td>
<td>261 ± 6</td>
<td>198 ± 6</td>
<td></td>
</tr>
<tr>
<td>WG05</td>
<td>4.2 ± 0.15</td>
<td>296 ± 4.11</td>
<td>4.1 ± 0.003</td>
<td>372 ± 6</td>
<td>276 ± 6</td>
<td></td>
</tr>
<tr>
<td>WG07</td>
<td>3.7 ± 0.15</td>
<td>293 ± 4.33</td>
<td>4.3 ± 0.003</td>
<td>237 ± 6</td>
<td>170 ± 6</td>
<td></td>
</tr>
<tr>
<td>WG08</td>
<td>3.0 ± 0.15</td>
<td>288 ± 3.70</td>
<td>3.7 ± 0.003</td>
<td>280 ± 6</td>
<td>224 ± 6</td>
<td></td>
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</table>
nearest-neighbour events starting from the fault centre (Silverman 1986). We determined the density of the individual samples, which is proportional to the fault-normal distance of the \( N \) th event. The density was then normalized by the total fault area and experiment duration. Changes in the sample size, \( N \), mainly influence the data scatter, and the characteristics within the distribution tail, whereas the slopes remained stable (see Fig. S2). Prior to AE density estimates, we stacked the AE activity from both sides of the faults and test for symmetry of AE event distributions relative to the fault axis. The symmetry test involves comparing the cumulative fault-normal-distances from each side of the fault and computing the maximum Kolmogorov–Smirnov (KS) distances for a set of possible fault centre locations. The ‘true’ fault axis minimizes the KS-distance between both fault sides. Details about the estimation of AE density distributions and sensitivity to fault orientation and centreing can be found in the supporting information.

The fall-off in AE density distributions could be described by a power law. The power-law exponents were determined using a maximum likelihood estimate (e.g. Newman 2005; Clauset et al. 2009). The corresponding minimum bounds were computed through maximizing the fit between observed and modelled, power-law-distributed data. The best-fitting power-law parameters minimize the KS distances between the observed and the modelled cumulative distributions (Clauset et al. 2009). We tested the statistical significance of the power-law fits by bootstrap resampling. To this aim, we created 10 000 synthetic data sets based on the estimated power-law parameters and compute the goodness-of-fit between synthetic data and the model as well as empirical data and the model. The resampling method evaluates how much of the difference between the model and the data can be explained by random, statistical variations as opposed to systematic variations, for example, due to applying an incorrect model. Following Clauset et al. (2009), we chose a significance level of 0.1 as sufficient to establish the power-law hypothesis. We tested the influence of hypocentral uncertainties on power-law distributions using synthetic data (Goebel et al. 2014). Close to the fault, the convolution of power-law and Gaussian uncertainties is controlled by location uncertainties whereas at larger distance the power law dominates the distributions. The more distant portion of the distribution can be used to estimate the power-law parameters and the influence of the Gaussian can be removed by a simple linear correction using the expected uncertainty, if both uncertainty and power-law exponent are not very large. The synthetic tests also revealed that the minimum power-law bound can lie slightly beneath the hypocentral uncertainties. A more detailed description of the here employed tests for power-law behaviour and corresponding parameter estimates can be found in Goebel et al. (2014).

3 RESULTS

Stick-slip type fault motion is characterized by increasing stresses during interslip periods and an abrupt decrease during failure, which can be considered a laboratory analogue to natural earthquake behaviour (e.g. Brace & Byerlee 1966). We strove to mimic the natural faulting process through creating series of stick-slip events on structurally complex fault zones allowing for abrupt earthquake-like stress release and fault evolution over several seismic cycles. As a consequence, the differential–stress curves during our experiments were generally characterized by: (1) A gradual stress increase which was linear at first and progressively deviated from linearity closer to failure and (2) sudden stress drops with magnitudes ranging from 4 to 220 MPa (Fig. 1). We observed two different groups of stress drop events: large stress drop (LSD) events with magnitudes between 118 and 220 MPa and small stress drop (SSD) events with magnitudes from 4 to 65 MPa. The characteristics of stress release of the current experiments differ from tests on planar, saw-cut surfaces (Goebel et al. 2014) during which predominantly linear stress increases alternated with LSD events. This suggests a direct relation between structural complexity and stress-curve complexity observed before failure, which were present during the current tests on natural-rough, fractured surfaces but absent during saw-cut surface experiments. In Sections 3.2 and 3.3, we examine fault structural complexity and connected changes in AE densities with fault-normal distance and successive stick-slip events in more detail. Periods between successive stick-slip events will be referred to as interslip periods (ISPs). The result section is organized as follows. Initially, we examine generic characteristics of AE hypocentre locations, fault structures, and AE density distributions. We then test changes in AE densities with successive stick-slips exemplified for experiment WG04, and then for all other experiments. Finally, we analyse differences in off-fault AE density distributions between individual experiments and discuss possible mechanisms, for example, differences in fault formation history and fault normal stresses.

3.1 AE hypocentre locations

The observed AE event populations enable monitoring of regions of local failure stress exceedance and connected micro-fracture processes. They also outline the approximate fault-zone extent and orientation within resolution limits and location errors. Fig. 2 shows AE event locations during the three ISPs of experiment WG04, displayed in the corresponding, best-fitting fault coordinate system \([X, Y, Z]\) denote coordinates in-plane slip-orthogonal, slip-normal and slip-parallel directions). AE events generally highlight a zone of high strain and brittle deformation, that is, the fault zone that developed from an initial fracture surface. While much of the deformation is localized within a planar zone connecting the two saw-cut notches, we also observed a diffuse zone of AE activity that extended out to larger fault normal distances. Furthermore, the AE event cloud indicates some degree of fault curvature and variations in fault zone widths along the \(Z\)-axis from 10 to 20 mm. Additional to \([Y,Z]\) fault curvature, we observed some AE activity towards the
Figure 2. AE hypocentres of experiment WG04 projected into a best-fitting fault coordinate system and viewed in a plane parallel and perpendicular to the fault. Left-hand column: fault-parallel view of AE events. The approximate fault extent is highlighted by a grey ellipse. The grey, dashed lines mark the approximate location of the notch tips. Centre column: AE events within a fault-perpendicular plane (see inset on bottom left-hand side). The extent of the saw-cut notches is indicated by grey bars at the top and bottom. Right-hand column: AE events within a fault-perpendicular plane viewed from the top of the sample. Each row marks a different interslip period of experiment WG04 labelled from ISP1 to ISP3 from top to bottom analogous to Fig. 1. Dots are coloured by magnitude.
Fault evolution and acoustic emission distributions

Figure 3. Example of fault zone extent after fracture and subsequent stick-slip sliding during experiment WG07. (a) Photographic image of the centre of the post-experimental fault zone. The width of the core deformation zone \( w_f \) varied between 1 and 3 mm along the direction of slip. White arrows indicate the direction of maximum compression. (b) CT-scan of the same fault area as in (a). Black, linear features highlight extent of core deformation zone that consists of sets of anastomosing cracks. The CT-scan images confirmed a core deformation zone width between 1 and 3 mm. The large crack outside of the core deformation zone (upper right) was formed early during the experiment and was active only during initial periods. (c) Microscopic image of thin section of the red rectangular region highlighted in (c). The core deformation zone contains ultrafine-grained gouge, larger clasts and pervasive microcrack damage, as well as one or more principle slip zones. The minimum width of the core deformation zone was between 1 and 1.5 mm. Outside of this zone, we observed a network of microcrack damage that was present in most of the thin section.

sample boundary \([Z_f = -20 \text{ mm}, Y_f = 15 \text{ mm}]\) in the upper frame of Fig. 2] likely connected to secondary faulting. The highest AE activity was observed during the first ISP whereas later ISPs showed less activity and more pronounced AE clustering within localized fault regions.

3.2 Fault structure and average AE density distributions

In the following, we investigate fault structural characteristics and damage-zone widths inferred from post-experimental microstructure images and fault-normal AE event density distributions, exemplified for experiment WG07. Thin-section images of the laboratory-created fault zones revealed zones of highly strained material within the fault core consisting of fault gouge, larger clasts (up to \( \sim 0.1 \text{ mm} \)) and one or more principle slip surfaces. These zones are embedded into highly fractured host rock. The density of micro fractures decreased as function of distance from the core deformation zone (see also Goebel et al. 2013b). The width of the core deformation zone could be identified within individual fault-orthogonal planes in photographic and CT images (Figs 3a and b), revealing strong variation along fault-strike. The maximum extent is up to \( \sim 3 \text{ mm} \) but may also be higher if additional principal slip surfaces are present. Principal slip surfaces, which have estimated widths on the order of tens of micrometres, exhibit a complex behaviour: diverging and joining together in different fault regions enclosing larger clasts between anastomosing branches. The enclosed material is commonly strongly fractured and shows local evidence of shear. The minimum extent of the core deformation zone was \( \sim 1 \text{ mm} \) (Fig. 3c), however, this width is also difficult to constrain due to the inherent incompleteness of 2-D representations of a 3-D, structurally complex fault zone. Thus, the
minimum width may even be lower in zones of highly localized deformation. Moreover, the displayed fault structure is the result of sample fracture and subsequent stick-slip events. The initial fault creation may already produce some microcrack damage within the fracture process zone (Vermilye & Scholz 1998; Janssen et al. 2001). Thus, the post-experimental structural analysis provides a cumulative picture of the created damage rather than resolving damage caused by individual stick-slip events.

To obtain a more detailed picture of step-slip related damage, we tested a possible connection between fault structure and average AE density distributions. The latter were initially estimated for AE events of all ISP sets. Events within a 8–20 s time window after slip onsets, showed a pronounced Omori-type aftershock decay (Goebel et al. 2012, 2013b). The aftershocks together with AE events that were associated with slip events were excluded from the current analysis because, here, we are interested in damage creation during stress increase on rough faults.

AE densities were determined using the same sample size (N = 30) for all experiments to ensure comparability of the results. We tested different values for N ranging from 10 to 240 which resulted in varying degrees of smoothness of density distributions and a slight decrease of the maximum extent of AE densities for the largest values of N, while the rate of special decay of AE densities remained largely unchanged (see Fig. S2). The AE density in our experiments was generally high close to the fault axis and remained at approximately constant values out to distances of several millimetres, for example, ∼2 mm for WG04 (Fig. 4). The constant, high AE activity indicates strong brittle deformation within this zone. At larger distances, the AE-density decay could be described by a power law. The power laws were bounded by the parameters Y min and Y max (Fig. 4). The former marks the transition between high AE activity within the core deformation zone and the power-law decay in AE activity. Y max marks the transition to a zone of secondary, seismic activity. This activity is likely not directly connected to the deformation along the fault but could rather be caused by large secondary cracks, or pre-existing material heterogeneity. In our experiments, quantitative estimates of Y max are impossible if the transition to the secondary activity occurs at large distances, or if the secondary activity is low. Consequently, the following analysis and interpretation are largely based on the power-law exponents, γ, and the minimum bounds, Y min, which can be estimated more reliably. In addition, we determined the parameters γ max which shows the variation in γ as a function of different values for the lower power-law bound, and γ, which is the power-law exponent corrected for hypocentral uncertainties.

The core deformation zone widths, w f , and the minimum power-law bound, Y min, varied systematically with the length of the saw-cut-guided, fracture surface, l RS (Table 2). Longer, rough surfaces were generally connected to larger maximum values of w f . Similarly, Y min increased as a function of l RS for all experiments, except for WG05. The increase in Y min highlights that longer, initially rough surfaces led to broader damage zone widths and broader zones of high AE activity. Experiment WG05 showed lower values for both power-law exponent, γ, and Y min than expected from the corresponding values of l RS and w f , which will be explored in more detail in Section 3.4.

The width of the zone of high AE activity, which is approximately 2Y min because of the profile stacking from both sides of the fault, is generally wider than the estimates of w f . This difference in width can be explained by a previously identified lower resolution between optical and AE methods (Zang et al. 2000). Optical methods generally have a lower resolution so that the AE hypocentre locations resolve damage structures out to larger fault-normal distances. Nevertheless, the initial comparison between fault zone structure and fault-normal AE density distributions shows interesting parallels, for example, the pronounced zone of high brittle deformation seen in both the microscopic images and high AE event densities close to the fault axis. This zone transitions into a power-law fall-off in AE densities and a region of decreasing microcrack densities observed in thin-section images.

### 3.3 Changes in density distributions and off-fault activity exponents with successive stick-slip events

We explored variations in the spatial decay of AE density distributions with successive ISP sets starting with experiment WG04. The initial ISP of experiment WG04 showed a plateau of AE density close to the fault axis out to a distance of about 2 mm (Fig. 5, top panel). Further out, a roll-off region occurs between 1.5 and 2.3 mm, and a power-law decay out to distances of Y f ∼7 mm. Secondary AE activity was also visible but did not influence the power-law slopes close to the fault. This observation was confirmed by computing power-law exponents without the region of secondary cracking. The power-law exponents increased systematically with successive stick-slip events, that is, a relatively larger proportion of AEs appeared closer to the fault highlighting a faster spatial decay during later ISP sets (Fig. 5).

To investigate the characteristics of individual density distributions in more detail, we computed the power-law exponent, γ , as function of varying minimum power-law cut-offs, Y min (Fig. 5, insets). In case of power-law distributed data, we expect to observe

<table>
<thead>
<tr>
<th>Sample</th>
<th>w f (mm)</th>
<th>Y min (mm)</th>
<th>l RS (cm)</th>
<th>γ</th>
<th>p-Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>WG04</td>
<td>1–4.2 ± 1</td>
<td>3.8</td>
<td>5.0 ± 0.15</td>
<td>3.2 ± 0.07</td>
<td>0.18</td>
</tr>
<tr>
<td>WG05</td>
<td>1–4 ± 1</td>
<td>0.9</td>
<td>4.2 ± 0.15</td>
<td>1.9 ± 0.01</td>
<td>0.15</td>
</tr>
<tr>
<td>WG07</td>
<td>1–3 ± 1</td>
<td>2.0</td>
<td>3.7 ± 0.15</td>
<td>3.1 ± 0.03</td>
<td>0.45</td>
</tr>
<tr>
<td>WG08</td>
<td>0.5–2.5 ± 1</td>
<td>1.6</td>
<td>3.0 ± 0.15</td>
<td>2.1 ± 0.02</td>
<td>0.11</td>
</tr>
</tbody>
</table>

Figure 4. Example of AE density distribution (blue circles) as function of fault-normal distance for experiment WG07. The blue line depicts the fit of the power-law distributed data between the power-law bounds marked by Y min and Y max (vertical, dashed lines).
Figure 5. AE event density as function of fault-normal distance for the three ISPs of experiment WG04. Power-law exponents are displayed next to the straight solid lines in each frame and minimum bounds of the power laws are highlighted by triangles. The insets show changes in $\gamma$ for different values of $Y_{\text{min}}$ and the corresponding KS-distances, that is, the minimum between distances between modelled and observed distributions (see text for details). The best-fitting $Y_{\text{min}}$ value (black dashed lines in inset) minimizes the KS-distance. The corresponding $\gamma$-values are marked by horizontal, coloured, dashed lines within the insets.
a rapid increase in $\gamma^*$ below $Y_{\text{min}}$, followed by largely constant values over the extent of the power law and larger fluctuations in the distribution tail. The corresponding Ks-distances for different values of $Y_{\text{min}}$ show a minimum at the beginning of the $\gamma^*$-plateau in agreement with the expected $Y_{\text{min}}$ values (Fig. 5, inset). The $\gamma^*$ values increased systematically over the whole range of $Y_{\text{min}}$ with subsequent ISPs emphasizing the robustness of the evolutionary trend. The range of the power-law behaviour remained approximately constant over the series of stick-slips based on an assessment of the respective ISP. The green dashed line represents an extrapolation for experiment WG04 using an exponential function of the form: $\gamma = A - B \exp(-Cn)$, where $A$, $B$ and $C$ are empirical fitting parameters, and $n$ is the respective ISP.

The CT-images generally depict the cumulative damage creation due to sample fracture and subsequent stick-slip events. The CT-scans revealed slightly larger fault angles for WG05 compared to WG07. Furthermore, we observed a comparably broad zone of high crack-density for experiment WG05 whereas WG07 showed a more localized core deformation zone (Fig. 8 insets). To compare these results to our prior estimates of $\mu$, we highlighted the corresponding angles in both CT-images. The damage-zone orientation and width within the CT-scan of experiment WG05 highlight a likely migration of the principle slip surface from 40° to 35° during successive stick-slip events. The damage-zone width of WG07, on the other hand, is comparably narrow, underlining the pronounced stability of principal slip surface orientations and $\mu$. Our estimate of $\mu$ based on AE hypocentres was $\approx 1^\circ$ lower than expected from CT-images, but is in agreement with a possible range of $\mu \approx 27^\circ - 30^\circ$ based on the observed width of the fault zone in Fig. 8. Due to the cumulative character of the damage within the CT-images a precise estimation of the fault angles for each ISP is complicated. Nevertheless, the slightly larger angle between fault and loading axis for experiment WG05 together with the broader damage zone support the previously suggested differences in $\mu$ between WG05 and WG07.

### 3.4 Changes in off-fault activity exponent with normal stress

Based on the variations in fault angle and the relatively large differences in effective, rough surface area (i.e. the fault area between...
the pre-cut notches), we also expect the stress level on the faults to differ between experiments. To investigate the influence of normal stress on seismic off-fault activity, we computed shear and normal stresses (see Table 1) corrected for both notch lengths and fault displacements. We then compared stress estimates to average off-fault activity exponents. To this aim, we compiled the AE events of all ISPs and computed AE density profiles but again excluded events within initial ISPs which showed the strongest deviation from the average $\gamma$ values. We observed a general trend of lower off-fault activity exponents with increasing normal stress so that $\gamma$ and $\sigma_n$ show a negative, linear relationship (Fig. 9). The corresponding Pearson’s correlation coefficient was estimated at $r = -0.93$ (Spearman’s rank $= -0.80$). Larger normal stresses result in a relatively larger proportion of off-fault activity which are associated with the relatively low $\gamma$-values, for example for experiment WG05, which experienced the largest fault stress level and a comparably slow off-fault activity decrease.

Table 3 presents an overview of off-fault activity exponents, corresponding goodness-of-fit ($p$-values) and the AE rate for individual experiments. In Goebel et al. (2014), we investigated the influence of hypocentral uncertainties on power-law parameters of the off-fault activity decay, and we find a linear increase in both $\gamma$ and $Y_{\text{min}}$ as function of hypocentral uncertainty, if the latter follows a normal distribution. The power-law exponents, $Y_{\text{corr}}$, corrected for hypocentral uncertainties, are displayed in Table 3, as well as in Fig. 9 assuming an average hypocentral uncertainty of $\sim$2 mm, and are the basis of the following discussion.

4 DISCUSSION

4.1 Relating fault structure and AE density distribution

Our results suggest a close connection between fault structure and AE density distributions. The density distributions are characterized by a zone of constant, high AE density close to the principal slip surface, a roll-over region, and a zone of rapid activity decay which could be described by a power law. Within a previous experimental series, we showed that the power-law decay is controlled by both fault roughness and fault normal stress (Goebel et al. 2014). Through analysing sets of post-experimental thin-sections, we quantified the connection between fault structure and resulting AE density characteristics (Fig. 10). The high AE density plateau is connected to strong brittle deformation within the fault core which is dominated by fine-grained gouge, large, elongated clasts (up to $\sim$0.1 mm) and zones of localized slip. We observed a
transition damage zone between highly deformed fault core and host-rock that showed pervasive fracturing and evidence of local shear deformation. Progressive damage accumulation likely led to a widening of the transitional damage zone as well as an increase in shear deformation. Progressive damage accumulation likely led to host-rock that showed pervasive fracturing and evidence of local transitional damage zone between highly deformed fault core and host-rock that showed pervasive fracturing and evidence of local shear deformation. Progressive damage accumulation likely led to a widening of the transitional damage zone as well as an increase in shear deformation.

4.2 Mechanisms of power law distributed off-fault activity

We observed a systematic change in \( \gamma \) with increasing normal stress and successive stick-slip events. The latter highlights the connection between off-fault activity, and fault evolution in form of roughness reduction with larger displacement. The influence of roughness and normal stress on the off-fault activity can be understood within the context of varying asperity-size distributions on material interfaces: Higher normal stresses on rough faults result in an increase in effective contact area and a relative higher proportion of large asperities (Dieterich & Kilgore 1996; Goebel et al. 2014). In addition, variations in fault roughness strongly influence the spatial decay of off-fault stresses (Dieterich & Smith 2009), and thus also the spatial decay of AE activity, if stress is mainly released seismically. Fault roughness and seismic-off-fault activity are related through the following equation (Dieterich & Smith 2009; Powers & Jordan 2010; Goebel et al. 2014):

\[
\gamma = c_s - H,
\]

where \( c_s \) is the geometric dimension, and \( H \) is the Hurst exponent of a fractal rough fault (see e.g. Mandelbrot 1982; Turcotte 1997). Goebel et al. (2014) noted that this is a more general form of the initially suggested model by Dieterich & Smith (2009), that accounts for the difference in asperity shapes and corresponding stress perturbations in 3-D. In 3-D, stress decays with distance \( r \) from an asperity as \( 1/r^3 \) as opposed to \( 1/r^2 \) in 2-D. Consequently, we expect the off-fault activity exponent to vary between 2 and 3 corresponding to Hurst exponents between 0 and 1 (Eq. 1). This expectation is approximately met by our observations (e.g. Fig. 11), although \( \gamma \) may reach values below 2 for rough faults that are loaded at high normal stresses. Surfaces with Hurst exponent of \( H = 1 \) are connected to a relatively larger proportion of roughness at large wavelengths compared to surfaces with \( H = 0 \) which show a larger proportion of roughness at small wavelengths.

4.3 Fault smoothing and the influence of normal stress and fault formation history

Our results show that fault evolution is complex even on incipient fracture surfaces in the laboratory. This complexity arises due to the interplay of fault roughness, stress and fault formation history. Changes in off-fault activity exponents, which were characterized by an initial increase over the first 1–3 ISPs, indicate strong fault smoothing at the beginning of the experiments. This is in agreement with a previous study during which we inferred a strong initial reduction in fault complexity based on decreasing fractal dimensions of AE hypocentre distributions (Goebel et al. 2013b). In that study, we observed fractal dimensions to decrease from initial values of 2.5 down to values close to 2. The latter is consistent with a predominantly planar distribution of AE hypocentres in 3-D and progressive fault smoothing. Fault smoothing is likely associated with the formation of zones of localized slip. These zones, which form after as little as 1–3 stick-slip events, were also observed in post-experimental experiments.
Table 3. Overview of off-fault activity and AE rate for the four experiments. \( \gamma \): off-fault activity exponent, \( \gamma_{\text{ave}} \): average power-law exponent and standard deviation for all ISPs except the initial ISP, \( \gamma_{\text{corr}} \): power-law exponent corrected for hypocentral uncertainty, \( p \)-value: goodness-of-fit of estimated \( \gamma \)-values, computed by Monte Carlo resampling, of the modelled distributions and comparing them to the observed distributions (Clauset et al. 2009). Within the scope of this study, we consider a power law a valid hypothesis for \( p \)-values above 0.10. \( N_{\text{AE}} \): total number of AE events, \( N_{\text{AE s}^{-1}} \): number of AE events per second.

<table>
<thead>
<tr>
<th>Sample</th>
<th>( \gamma )</th>
<th>( \gamma_{\text{ave}} )</th>
<th>( \gamma_{\text{corr}} )</th>
<th>( p )-Value</th>
<th>( N_{\text{AE}} )</th>
<th>( N_{\text{AE s}^{-1}} )</th>
<th>( N_{\text{LSD}} )</th>
<th>( N_{\text{SSD}} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>WG04</td>
<td>3.37 ± 0.15</td>
<td>3.45 ± 0.14</td>
<td>3.06 ± 0.14</td>
<td>0.21</td>
<td>17,363</td>
<td>4.58</td>
<td>3</td>
<td>5</td>
</tr>
<tr>
<td>WG05</td>
<td>1.84 ± 0.10</td>
<td>1.91 ± 0.08</td>
<td>1.84 ± 0.08</td>
<td>0.11</td>
<td>20,020</td>
<td>4.24</td>
<td>6</td>
<td>5</td>
</tr>
<tr>
<td>WG07</td>
<td>3.19 ± 0.12</td>
<td>3.27 ± 0.04</td>
<td>2.92 ± 0.08</td>
<td>0.18</td>
<td>27,797</td>
<td>3.51</td>
<td>6</td>
<td>8</td>
</tr>
<tr>
<td>WG08</td>
<td>2.58 ± 0.17</td>
<td>2.54 ± 0.09</td>
<td>2.44 ± 0.08</td>
<td>0.29</td>
<td>17,890</td>
<td>2.45</td>
<td>6</td>
<td>5</td>
</tr>
</tbody>
</table>

Within the scope of this study, we consider a power law a valid hypothesis for \( p \)-values above 0.10. \( N_{\text{AE}} \): total number of AE events, \( N_{\text{AE s}^{-1}} \): number of AE events per second.

thin-sections (e.g. Fig. 3). Within the present study, we observed a reduction in secondary cracking and associated AE activity with successive stick-slip events (see e.g. Fig. 5) indicating that off-fault damage seems to also progressively localize.

Experiment WG05 deviated from the other three experiments by showing consistently low \( \gamma \)-values and lacking the initial periods of fault smoothing. This could be explained by an interplay of fault formation and evolution effects: The freshly formed fracture surface for this experiment was connected to a comparably large fault angle which changed gradually with successive stick-slip events. The preferred fracture angle of Westerly granite is between 25–30° (e.g. Mogi 2007), which is in agreement with our experiments except for experiment WG05 (see Fig. S5). The fracture process of experiment WG05 may have been influenced by material heterogeneity or slight deviations in orientation and width of the saw-cut notches leading to \( \gamma \)-values which are higher than expected. The systematic changes in fault angle after the initial fracture process are likely related to changing slip surface orientations and a more favourable alignment with the principal stresses. Moreover, for this experiment, we observed a relatively wider damage-zone and large-wavelength anastomosing crack structures in post-experimental thin section and CT scans. The extent of the damage zone may be connected to repeated variations of principle slip surface orientations. Thus, a combination of initial fault zone orientation, and changes in fault zone structure due to stick-slip fault motion are likely responsible for the observed differences in characteristics of AE density distributions.

Goebel et al. (2014) observed that increasing fault normal stresses result in a decrease in \( \gamma \) for experiments on rough saw-cut surfaces. We compare these results with values of \( \gamma_{\text{corr}} \) from initial ISPs of the
current experimental series (Fig. 11). The two sets of experiments, including experiment WG05, can be described by a negative, linear relationship between \( \gamma_{corr} \) and \( \sigma_n \) (see squares and solid black line in Fig. 11). This relationship highlights the sensitivity of rough surfaces to variations in normal stress so that larger normal stresses generally lead to a slower spatial decay of AE events with respect to the fault axis. Besides the influence of normal stress, Fig. 11 also displays the evolution of laboratory faults with successive stick-slip events. Within the first 1–3 ISPs, the \( \gamma_{corr} \)-values increased rapidly (coloured ellipses in Fig. 11) reaching values similar to that of a smooth, polished surface (grey, dashed ellipse in Fig. 11). This similarity between \( \gamma_{corr} \) of relatively mature, fractures surfaces and polished saw-cut surfaces may also imply similar fault roughness. Consequently, the repeated rupture of natural rough surfaces over series of stick-slip events is likely connected to extensive surface smoothing, so that mature, gouge-rich faults show similar AE density decays to fresh, polished surfaces with little to no displacements. Based on the current set of experiments, we cannot resolve how generic the observed smoothing processes are, raising the question, whether all natural-rough surfaces eventually evolve into smooth faults, characterized by localized slip and decreasing spatial extents of off-fault activity.

Fault smoothing rates likely depend on the formation history and stress state of the fault. Roughness reduction may be most effective within a certain range of conditions, for example, high initial roughness and favourable alignment with the principle stress axes. The difference in the smoothing process is most easily seen for experiment WG05 which showed no evidence of fault smoothing within the present range of displacements. The current experimental series are limited to comparably small displacements and we cannot rule out that secondary smoothing processes will become active or observable after sufficient displacement has been accumulate. Despite these limitations, we observe many similarities between the statistics of AE events and natural seismicity. This highlights the importance of our results for the understanding of seismicity variations in nature.

### 4.4 Is fault evolution limited to small displacements?

A power-law decay in seismic off-fault activity is in agreement with a theoretical study Dieterich & Smith (2009) and a study of the spatial decay of seismicity in the proximity of natural faults (Powers & Jordan 2010). Powers and Jordan suggested that off-fault activity exponents decrease systematically with increasing displacements and fault smoothness even at large displacements of up to 300 km. Our results support progressive fault smoothing with successive stick-slip events, however, this process may not be continuous. Within the range of displacements of the current experimental series, we observed that faults rapidly reached an approximately constant value of \( \gamma \) suggesting that roughness remained at a stable level thereafter. Similar observations have been made for exhumed crustal fault zones, for which a reduction in roughness and extension of damage zone widths are predominately active within the first 10–100 m of cumulative fault displacements whereas above no evolutionary signal is observable (Sagy et al. 2007; Savage & Brodsky 2011; Brodsky et al. 2011). On the other hand, a reduction in fault stepovers and geometric disorder is observed even for faults with large cumulative displacements (e.g. Wensoulsky 1988; Wechslar et al. 2010) suggesting that evolutionary processes are active on mature faults.

The differences between laboratory and natural seismicity can possibly be attributed to additional complexity in structure and roughness of natural fault zones. Most of the off-fault activity exponents of natural seismicity fall within a range of 1–2 (Hauksson 2010; Powers & Jordan 2010). Powers and Jordan noted that this range of exponents is consistent with theoretical results for seismic off-fault activity in the proximity of fractal, rough faults in 2-D for which \( \gamma = 2 - H \) (Dieterich & Smith 2009). However, as pointed out in Goebel et al. (2014), in 3-D one expects the seismic off-fault activity to be related to the fractal roughness over \( \gamma = 3 - H \). The roughness of natural faults may be controlled by depth persistent structural features like fault stepovers. These stepovers likely introduce a roughness component that is approximately constant with...
depth and changes only along strike thus influencing the off-fault seismicity decay similarly to a fault in 2-D. Hence, fault-normal seismicity distributions are likely influenced by both surface roughness and structurally induced roughness which may explain the entire range of $\gamma$-values including high values of up to $\gamma = 3$ in Powers & Jordan (2010). This influence may also explain the apparent discrepancy between studies that propose fault smoothing to be continuous versus studies that propose smoothing to only be active at small displacements. Moreover, our experiments highlight the role of increased normal stresses which cause faults to appear ‘seismically rougher’, that is, they are characterized by a slower spatial decay of seismic off-fault activity.

5 CONCLUSION

We conducted four frictional sliding experiments on rough fault zones that evolved from incipient fracture surfaces. The laboratory-created faults showed many similarities to natural fault zones including a core deformation zone consisting of gouge and areas of slip localization as well as an off-fault damage zone with decreasing crack density at increasing fault-normal distances. We observed a connection between the characteristics of seismic-event density distributions and the structure of complex, laboratory-created faults. The core deformation zone was associated with consistently high AE activity whereas the off-fault damage zone showed a power-law AE density decay. The exponent of this power law is sensitive to normal stress and changes in fault roughness, and can be used to document fault evolution with successive stick-slip events.

The laboratory faults showed strong evidence for fault evolution during the initial 1–3 interslip periods as a consequence of fault smoothing and reduction in fault complexity. Over the following interslip periods, fault evolution was no longer observable based on variations in off-fault AE distributions. The lack of evolutionary signals suggests that fault smoothing processes are most effective during early stages of fault development. Relative differences in off-fault activity exponents between experiments were predominantly controlled by the normal stress on the faults revealing a linear relationship between normal stress and off-fault activity exponents for rough faults. Consequently, increasing normal stresses generally result in a relatively slower spatial decay of seismic off-fault activity.

Our results highlight that fault roughness, stress state, and formation history of a fault are important parameters that control near-fault seismicity distributions. Distinguishing between roughness- and stress-related variations in fault-normal distributions of natural seismicity may provide important insights into fault zone properties including along strike variations of frictional properties and stress.

ACKNOWLEDGEMENTS

We thank Stefan Gehrmann and Matthias Kreplin for the rock sample preparation at GFZ-Potsdam, Germany. The authors wish to thank the editor, Jörg Renner, and two anonymous reviewers for suggestions that helped improve an earlier version of the manuscript. This research was supported in part by the Southern Californian Earthquake Center under contribution numbers 11017 and 13022.

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