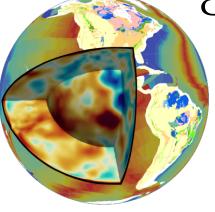
Geodynamics I: Subduction zone dynamics and global mantle flow



Thorsten W. Becker

The University of Texas at Austin

CIDER Summer School Subduction Zone Dynamics



Berkeley CA July 2017





Jackson School of Geosciences

Contents

- Plate driving forces
- Some fluid dynamics
- Global models
- Regional models
- Conveyor belts

Plate tectonics is the top boundary layer of mantle convection Subduction: cold plume dynamics



fluid heated from below - Rayleigh-Benard convection

computation by A. McNamara

- Rayleigh number, Ra, controls the vigor of convection
- Symmetry of upwellings and downwellings broken by
 - → temperature dependence of viscosity
 - → depth-dependent viscosity
 - → internal vs. bottom heating
 - → fractionation (e.g. continents and thermo-chemical piles)

Top thermal boundary described by half space cooling

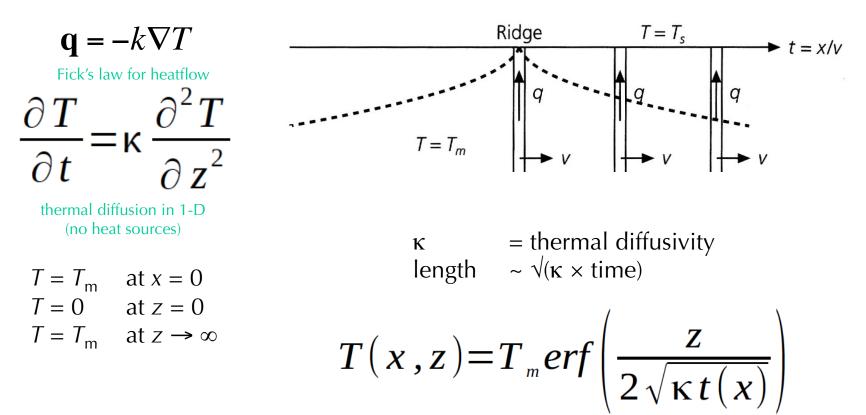
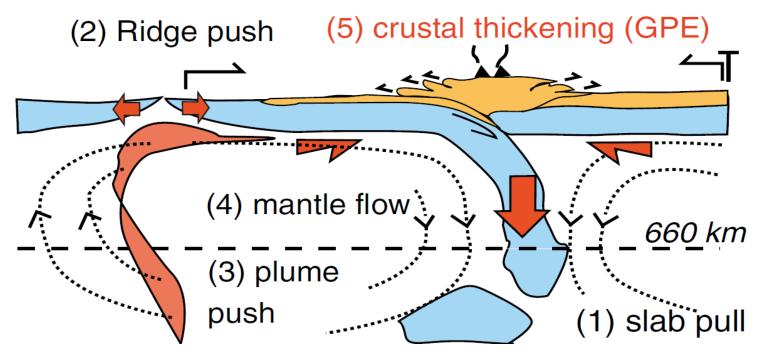
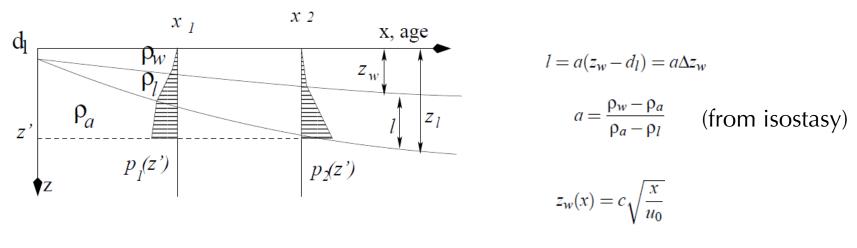


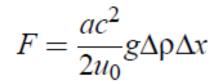
Plate driving forces: Integrals over components of thermo-chemical convection

GPE = gravitational potential energy

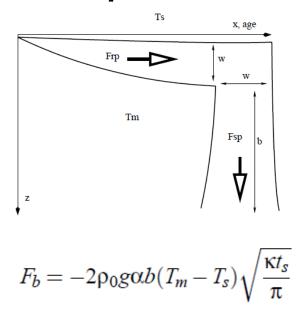


Lithospheric thickening (AKA *ridge push*, oceanic GPE)



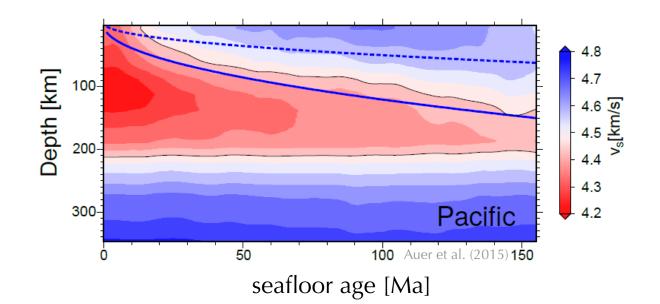


Subducting thermal boundary layer: Slab pull

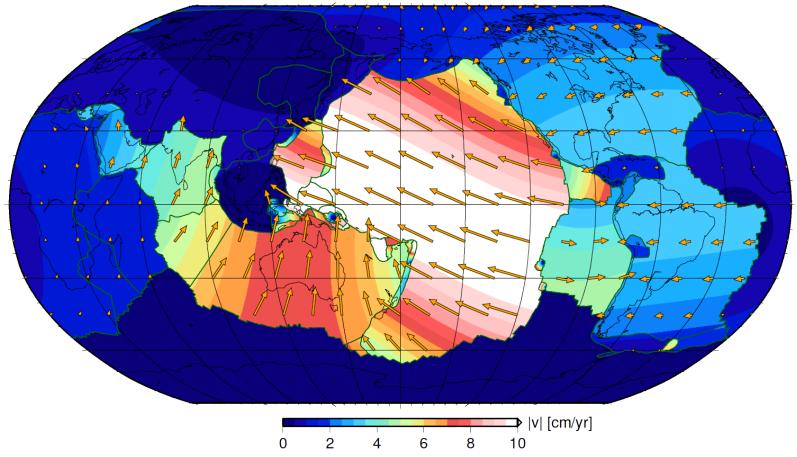


Force estimates from half-space cooling

- > ridge push (lithospheric thickening) ~ 10^{12} N/m
- > slab pull ~ 10^{13} N/m
- » worried about tectonics? worry about subduction



How to explain present-day plate tectonics and test our models?



Bird (2002) plate boundaries and MORVEL56 velocities by Argus et al. (2011) in spreading-aligned reference frame (Becker et al., 2015)

Different natural experiments in space: 120 60 total continental area/106 km2 Plate speed correlation with 100 area/106 km2 80 40various geometric/kinematic parameters 60 total plate a 20 40 Selferie Sudarding % energine the stand of the sta 20 [%] effective fige boundary 0 0 50 average true plate speed/mm y-1 average true plate speed/mm y-1 * continental (a) (b) Plate velocit Plate area 40 dary/ length of trenches attached (~slab pull Plate velocity length of effective % of total cir Plate area 0.50 gth of ef % of t % continental area 120 0 20 40 60 80 100 60 average true plate speed/mm y-1 average true plate speed/mm y-1 0.00 (c) (d) % effective subduction boundary 60 length of transform fault boundary/ % of total circumference (a) Eurasia (b) North America % effective ridge (c) South America -0.50(d) Antarctic boundary 40(e) Africa (f) Caribbean -0.75 (g) Arabian % effective transform (h) Indo-Australia boundary -0.90 20 (i) Philippine

King (2008)

correlation

-1.00

0

(e)

20

40

60

average true plate speed/mm v-1

80

100

120

Forsyth & Uyeda (1975)

(j) Nazca (k) Pacific

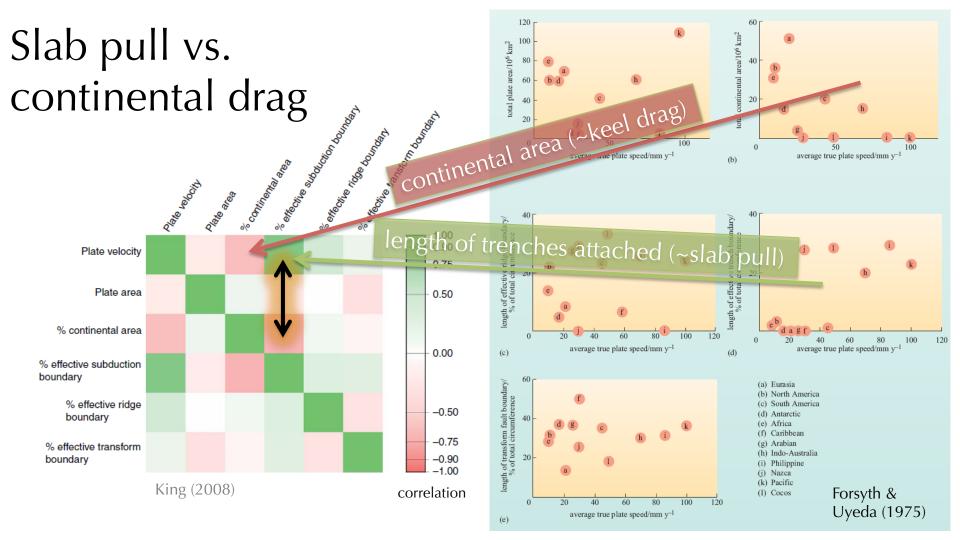
(I) Cocos

100

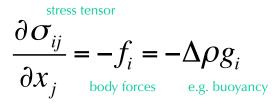
100

120

80



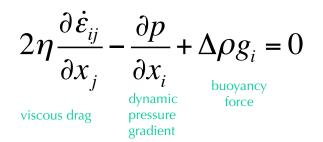
Some fluid dynamics to build our own models Static force balance (conservation of momentum) in any continuum



Constitutive law for an incompressible, Newtonian fluid

$$\frac{\partial v_i}{\partial x_i} = 0 \qquad \qquad \sigma_{ij} = -p\delta_{ij} + 2\eta\dot{\varepsilon}_{ij} = -p\delta_{ij} + \eta(\frac{\partial v_i}{\partial x_j} + \frac{\partial v_j}{\partial x_i})$$
conservation of mass
$$\overset{\text{dynamic}}{\underset{\text{pressure}}{\overset{\text{Newtonian}}{\overset{\text{viscosity}}{\overset{viscosity}{\overset{viscosity}{\overset{viscosity}{\overset{viscosity}}{\overset{viscosity}{\overset{viscosity}{\overset{viscosity}{\overset{viscosity}}{\overset{viscosity}{\overset{visty}{\overset{visc}{\overset{visc}}{\overset{visty}{\overset{visty}{\overset{visty}{$$

Stokes equation for constant viscosity (neglect inertia, OK at 10⁻²⁵ level (1/Pr))

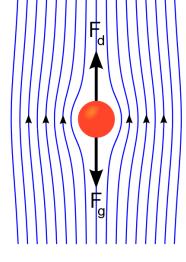


Stokes sphere / Stokes sinker

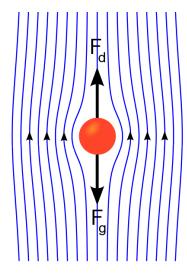
 F_d = area × stress = area × strain-rate × viscosity (η) = area × velocity (v)/radius (a) × viscosity

 F_g = density contrast ($\Delta \rho$) × gravitational acceleration (g) x volume

$$V_{\text{Stokes}} = C \frac{\Delta \rho g a^2}{\eta_m}$$



A Stokes solution: Stokes sphere

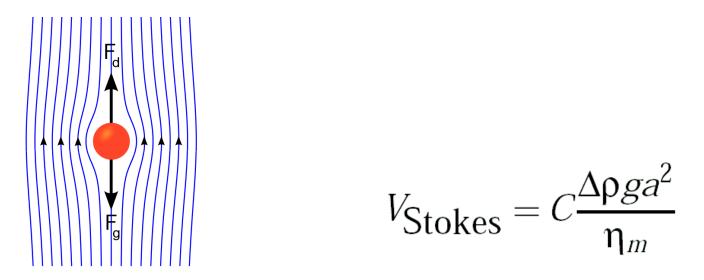


$$V_{\text{Stokes}} = C \frac{\Delta \rho g a^2}{\eta_m}$$
$$C = \frac{2 + 2\eta'}{6 + 9\eta'} \quad \eta' = \frac{\eta_s}{\eta_m}$$

Aside I:

 \rightarrow A needle, as opposed to sphere, will sink with 0.5...2 $v_{\rm Stokes}$

Stokes sets the advective scale



Aside II:

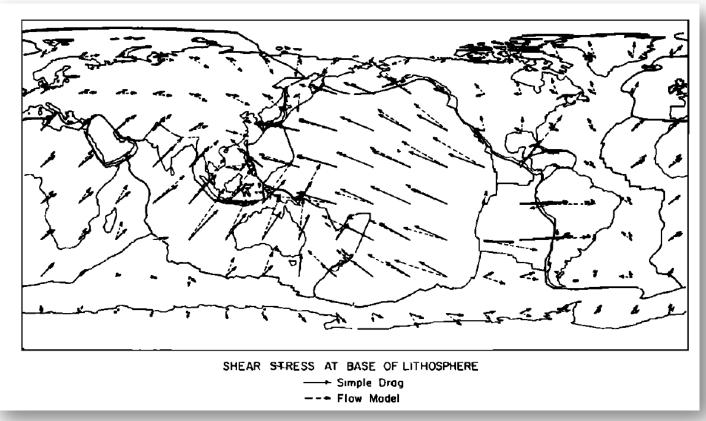
• Peclet# = ratio of diffusive to convective time scale, $Pe = t_{diffusion} / t_{convection}$

→
$$t_{\text{diff}} = a^2 / \kappa$$
, $t_{\text{conv}} = a / v_{\text{Stokes'}} \Delta \rho = \Delta T \alpha \rho_{0'}$ then $Pe \rightarrow Ra$ (with a instead of L)

Density driven flow

 $v \propto \frac{\Delta \rho}{\eta}$ $\sigma \propto \eta \dot{\varepsilon} \propto \eta \frac{v}{a} \propto \frac{\Delta \rho}{a}$

Plate motions and global mantle flow



Hager & O'Connell (1979)

Mantle circulation

- > treat mantle and lithosphere as a fluid
- > infinite Prandtl number (no inertia) approximation
 - Navier-Stokes turns into Stokes equation
- > instantaneous solution for given density and boundary conditions
 - can solve in < 1 s for spherical Earth without lateral viscosity variations

force balance (conservation of momentum) $\frac{\partial \sigma_{ij}}{\partial x_j} = -Ra\tilde{T}\delta_{ir}$ thermal buoyancy

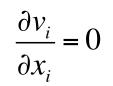
constitutive equation (rheology) and conservation of mass

Calculation Settings

onstant scaling factor

HC of SEATREE GUI is part of UGESCE or CIDER VirtualBox distribution

$$\sigma_{ij} = -p\delta_{ij} + 2\eta\dot{\varepsilon}_{ij}$$



Colors: Pbound vecto

Mantle circulation

- > Thermo-chemical heterogeneity and complex rheologies make things interesting
- Finite element methods best suited for lateral viscosity variations (can solve all of this, in ~hours, at < km resolution without approximations), with ~512 CPUs



force balance (conservation of momentum)

 $\frac{\partial \sigma_{ij}}{\partial x_{i}} = -Ra\tilde{T}\delta_{ir} + Ra_{C}\tilde{C}\delta_{ir}$ chemical buoyancy

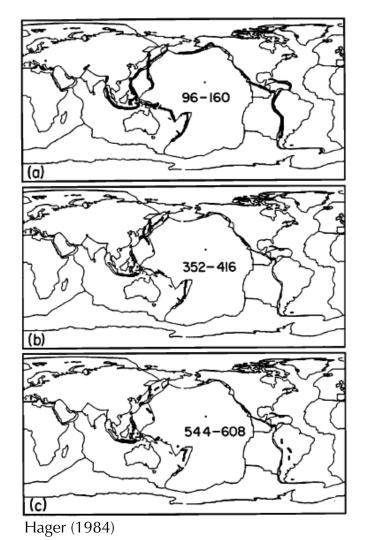
constitutive law (rheology)

 $\sigma_{ij} = -p\delta_{ij} + 2\eta(\sigma, T, d, H_2O, \varepsilon)\dot{\varepsilon}_{ij}$

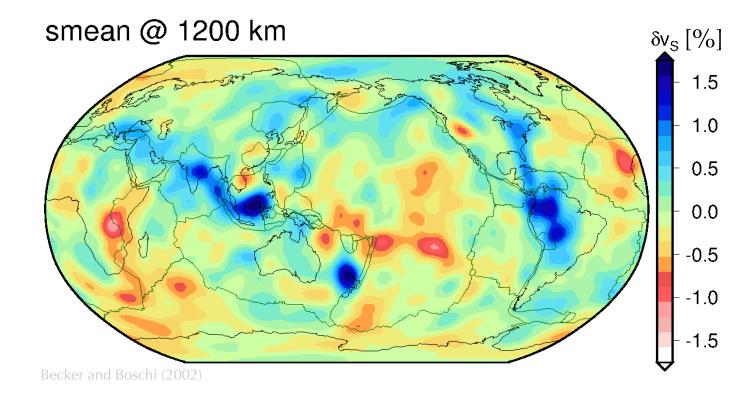
non-linear rheology

How do we know the density variations in the mantle?

upper mantle slabs from Wadati-Benioff zones

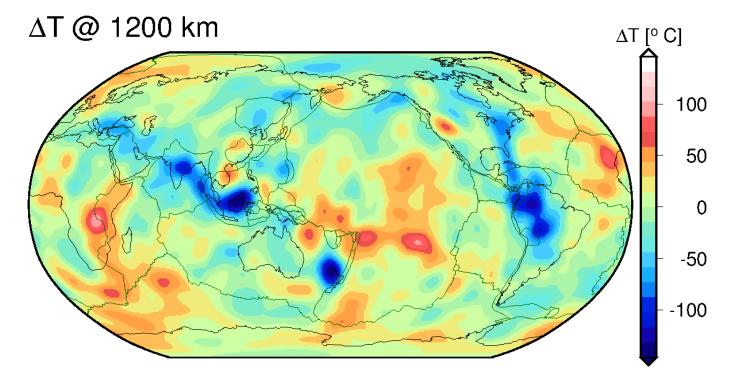


Seismic tomography also shows slabs



S wave models provide poor image of slabs in upper mantle
P wave models poor outside subduction zones in upper mantle

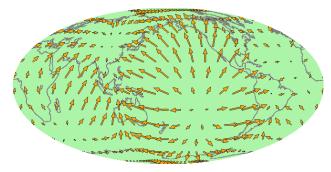
Besides cratons and piles: dln $\rho/d \ln v_s = 0.2$



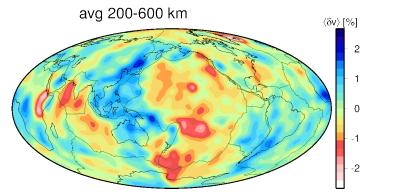
> Use mineral physics to convert velocity into temperature (density) anomalies

Tomography driven flow at surface

Flow model with free slip surface (no lateral viscosity variations)

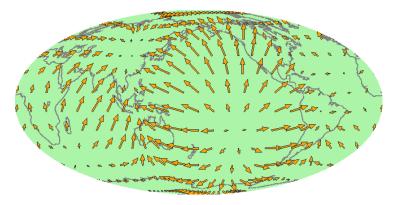


Upper mantle averaged tomography



Surface motions compared to plate motions

Flow model with free slip surface and no LVVS



Observed plate velocities in hot spot reference frame

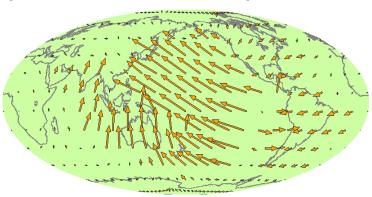
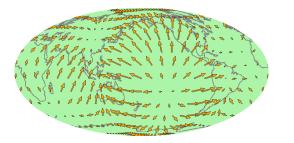
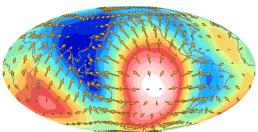


Plate motions require LVVs in lithosphere

Flow model with only radial viscosity variations

poloidal component



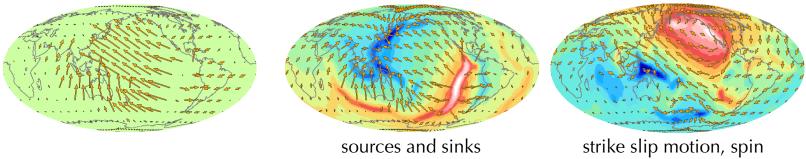


- No toroidal flow without lateral viscosity variations (no PT coupling)
- Strain-rates not very plate-like

toroidal component

Observed plate velocities in hot spot reference frame

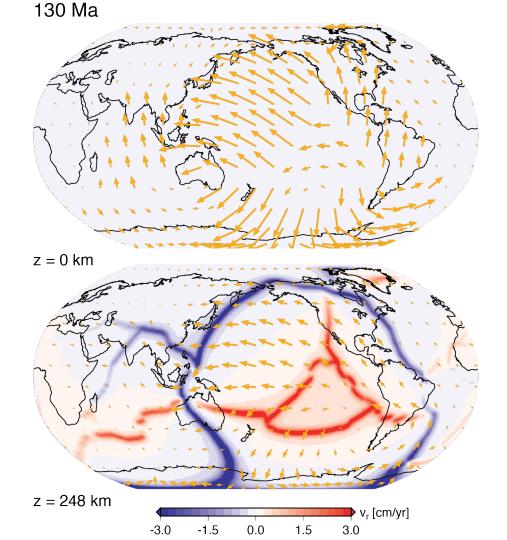
poloidal component



Ricard and Vigny (1989); O'Connell et al. (1991); Ricard et al. (1991); Ribe (1993); Forte & Peltier (1993); Thoraval & Richards (1997); Moucha et al. (2008); Ghosh et al. (2010)

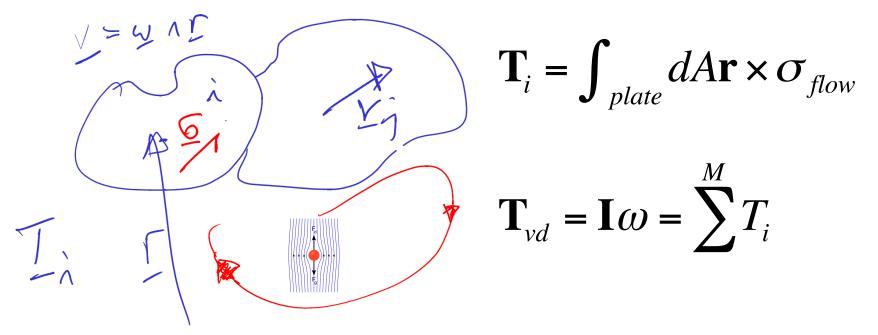
Plate-plate Interactions

can compute interaction matrices for arbitrary plate geometries and viscosity distributions



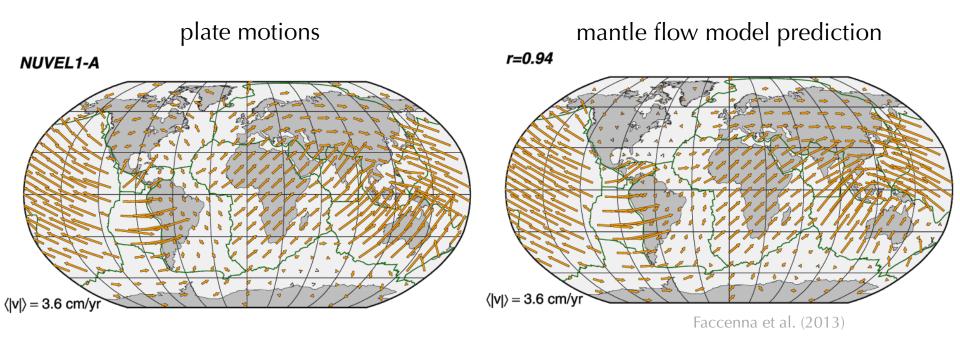
cf. Hager and O'Connell (1981), Ricard and Vigny (1989), Forte (1993)

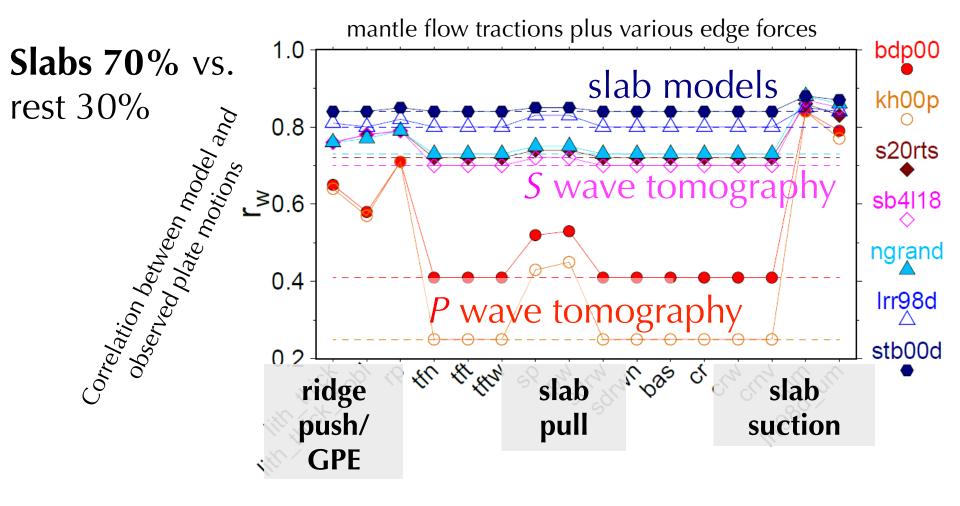
Solve for rigid plate motions given mantle tractions

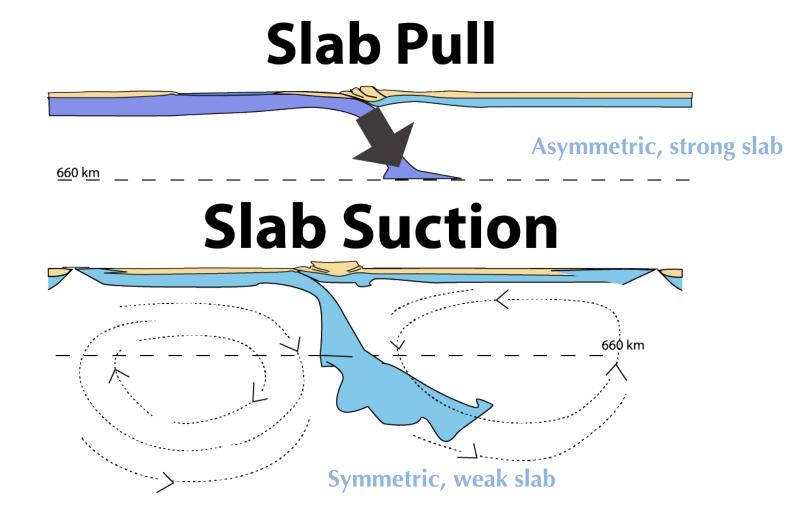


cf. Ricard and Vigny (1989); Forte (1993); Becker and O'Connell (2001) Conrad and Lithgo-Bertelloni (2002): van Summeren et al. (2010) *Note*: Can construct plate motion interaction matrix **I**, for any LVVs

Plate motion models ~work







cf. Conrad and Lithgow-Bertelloni (2002)

Plate speed vs. slab suction / slab pull

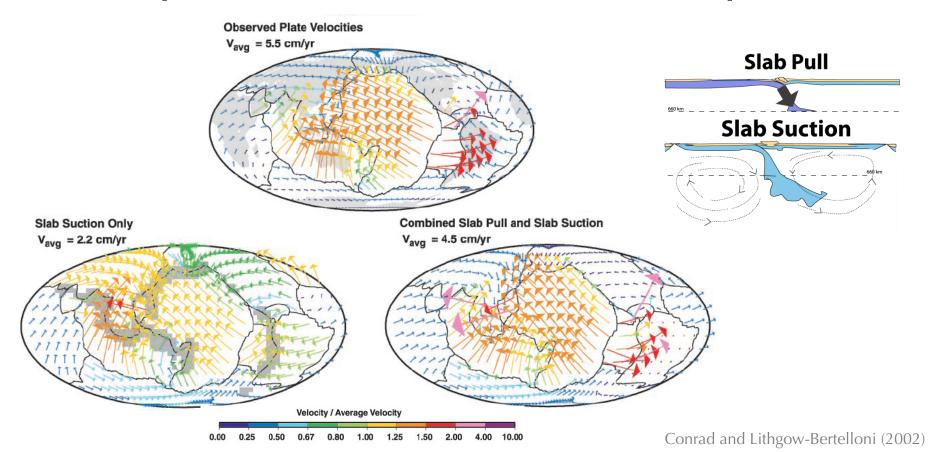
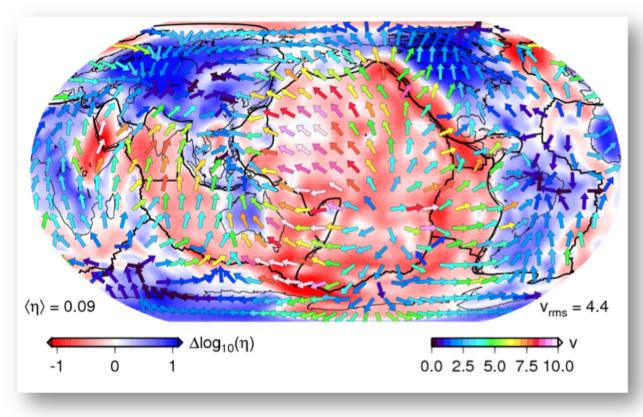


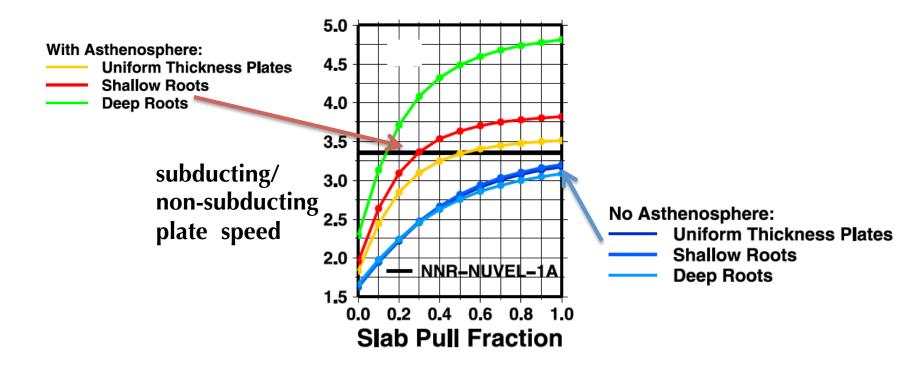
Plate speed vs. asthenospheric viscosity



cf. Ricard et al. (1993); Zhong (2000)

Becker (2006)

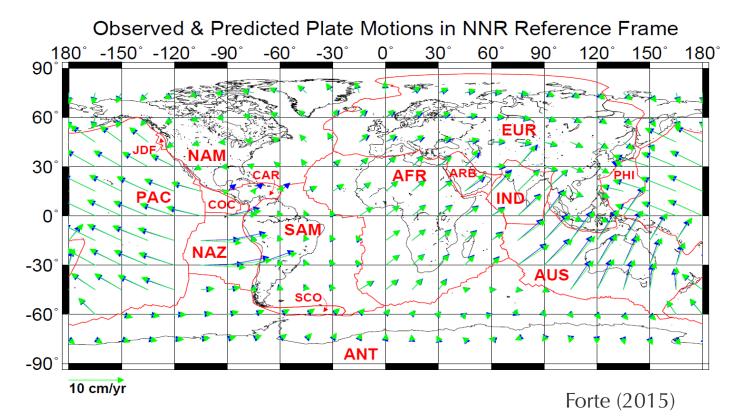
Asthenosphere vs. slab viscosity tradeoff



cf. Becker and O'Connell (2001); Conrad and Lithgow-Bertelloni (2002); Becker (2006)

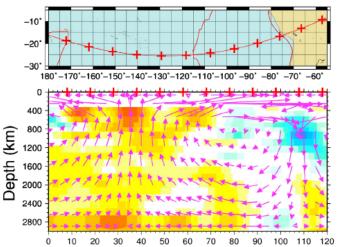
van Summeren et al. (2012)

Some more uncertainties

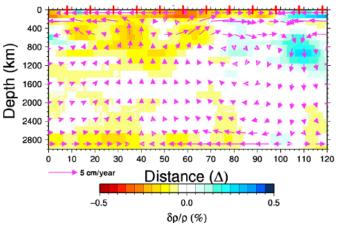




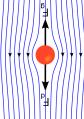
Importance of viscosity and density simple tomography to density scaling, simple viscosity structure Importance of (mineral physics, compositional anomalies)



C S20RTS dens. (from inversion) & V2 visc.

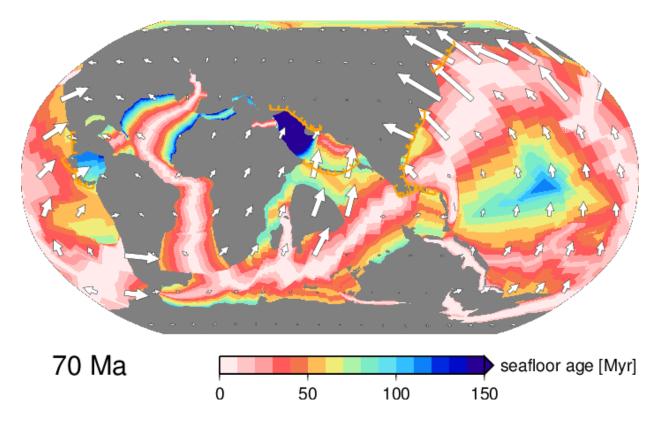


joint tomography / dynamics inversion for density, complicated viscosity structure



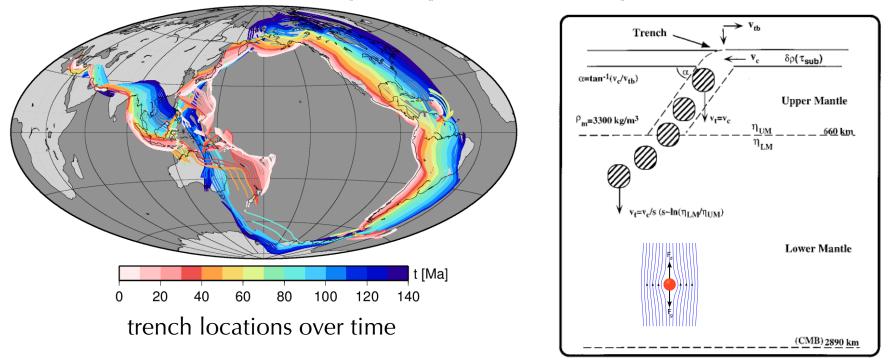
Rowley et al. (2016) cf. Simmons et al. (2009) Forte and Mitrovica (2004) Forte (2015)

Global plate tectonics experiments in the past



Mueller et al. (2016)

Stokeslets link subduction history and mantle viscosity to present-day structure



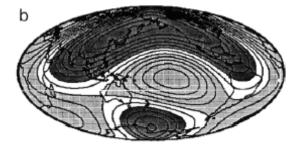
Steinberger et al. (2010)

Ricard et al. (1993); Lithgow-Bertelloni et al. (1993, 1998)

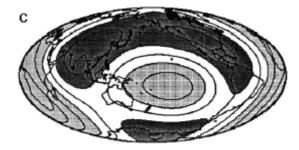
SLABS (DEPTH 2000 KM, DEGREES 1-15)



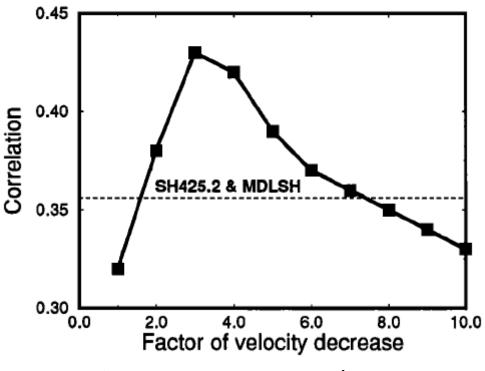
SLABS (DEPTH 2000 KM, DEGREES 1-3)



SH425.2 (DEPTH 2000 KM, DEGREES 1-3)

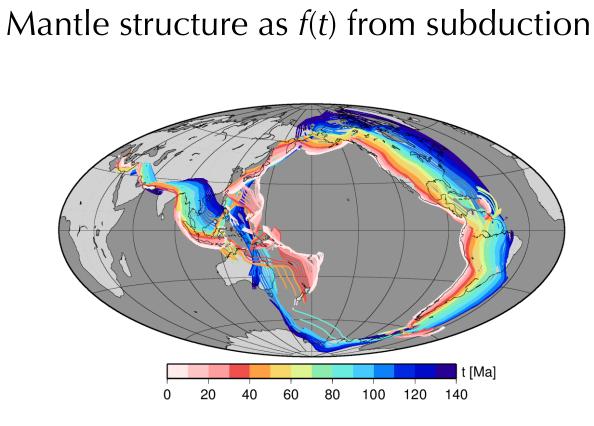


CORRELATION SLABS/SH425.2

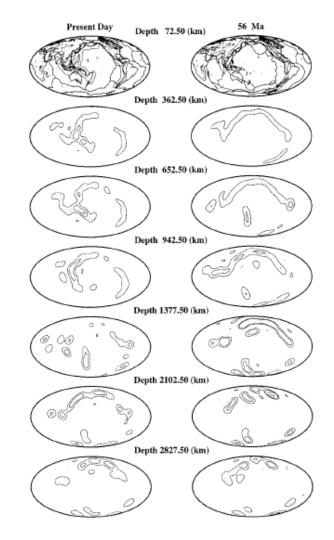


 constraint on upper/lower mantle viscosity increase

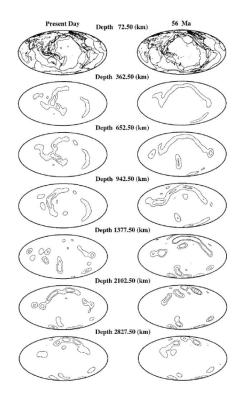
Ricard et al. (1993)

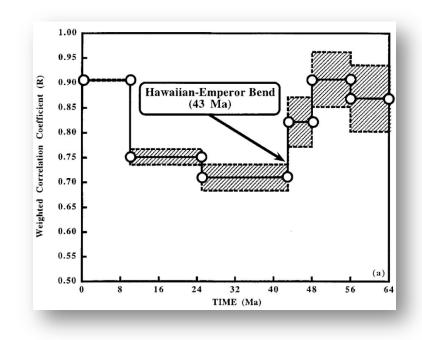


Ricard et al. (1993); Lithgow-Bertelloni & Richards (1998); Steinberger (2000); Spasojevich et al. (2009); Steinberger and Torsvik (2010) van der Meer (2010); Steinberger et al. (2014); Bower et al. (2015)



Time-dependent match to plate motions based on slablets

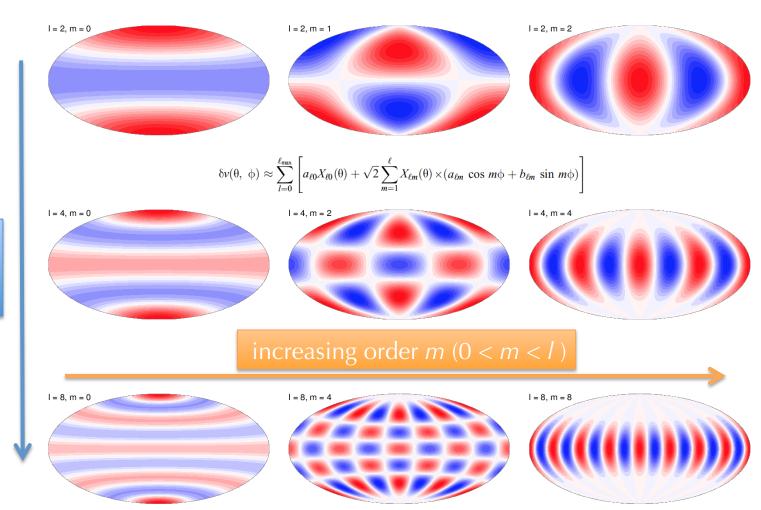




Lithgow-Bertelloni and Richards (1998)

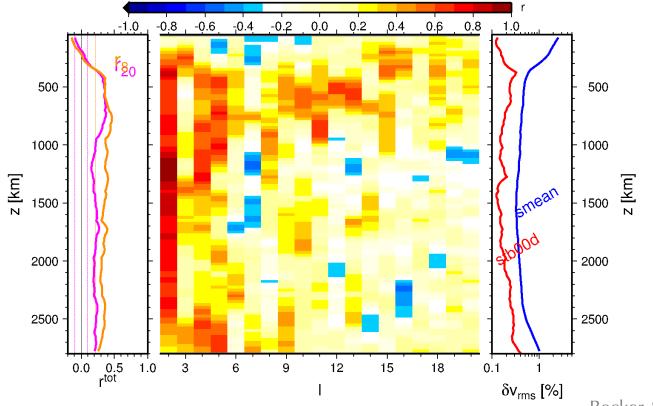
Spherical harmonics for analysis of global fields

> increasing degree / (1/wavelength)



Correlation of global slab model with tomography (does not work that well...)

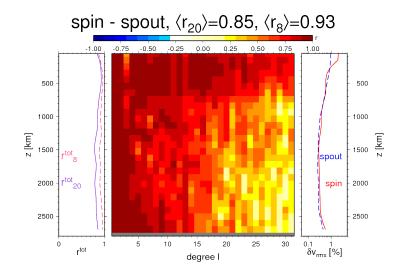
stb00d vs. smean, $\langle r_{20} \rangle = 0.21$, $\langle r_8 \rangle = 0.30$



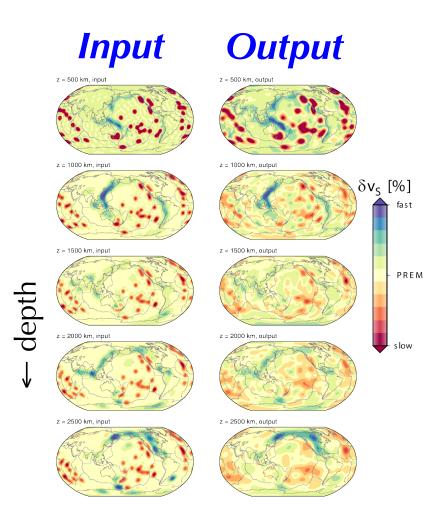
Becker & Boschi (2002)

Lithgow-Bertelloni & Richards (1998); Steinberger (2000); Bunge & Grand (2000); Spasojevic & Gurnis (2009)

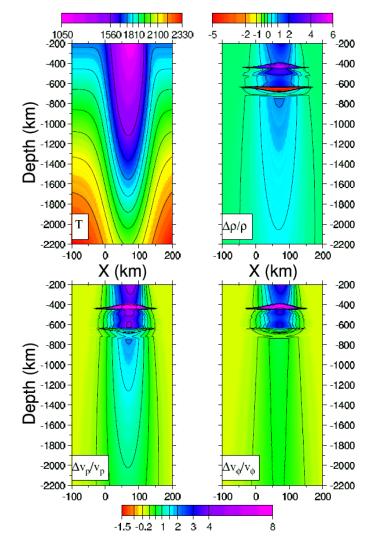
Seeing the slab I



Note: can resolve structure up to degree $I_{max} \sim 15$ in wave theoretical framework

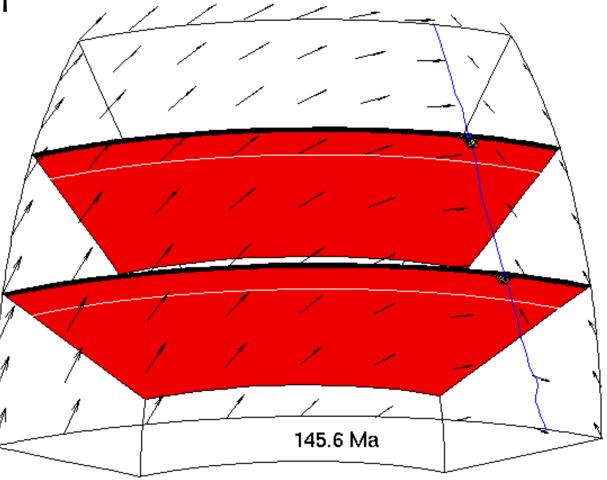


Seeing the slab II ?



Ricard et al. (2005)

Seeing the slab III ?

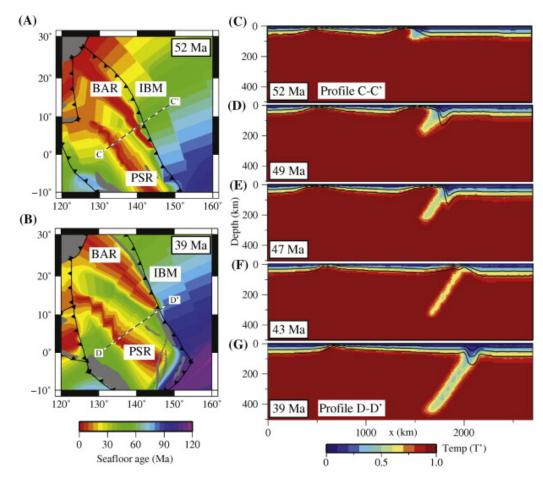


Tan et al. (2001)

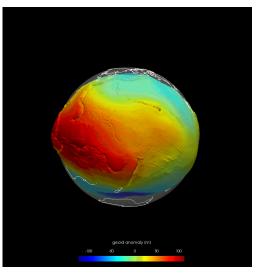
Slab models do not quite explain mantle structure, because of...

uncertainties about

- plate reconstructions
- \succ slab and mantle rheology
- \succ mineral physics and composition
 - \succ mass flux through 660
- ➤ active upwellings and thermochemical piles



Other constraints on slabs



vertically exaggerated EGM360 geoid

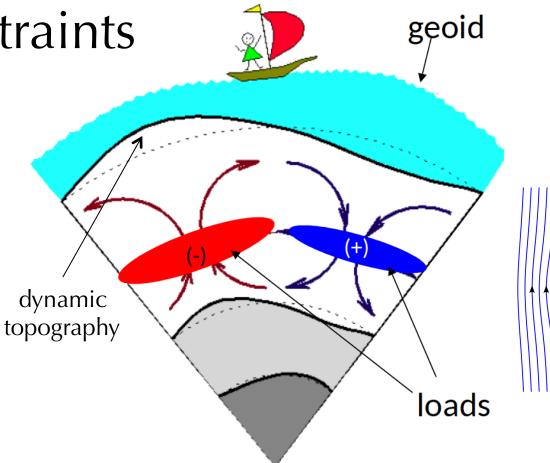
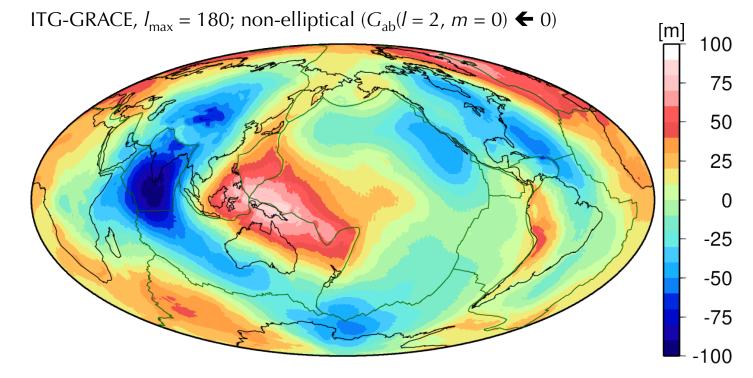


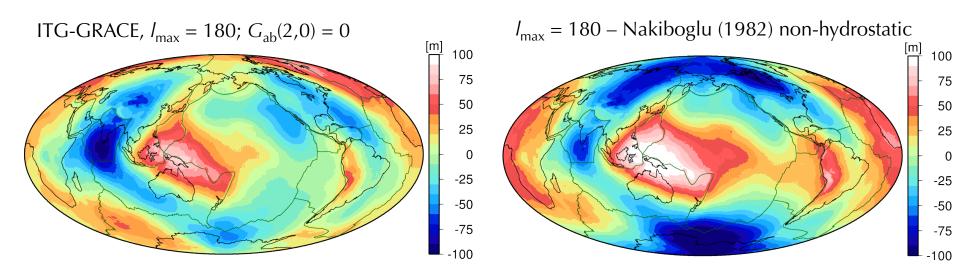
Figure from Y. Ricard

Geoid anomalies

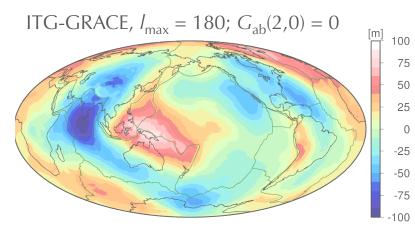


scale is saturated

Geoid anomalies

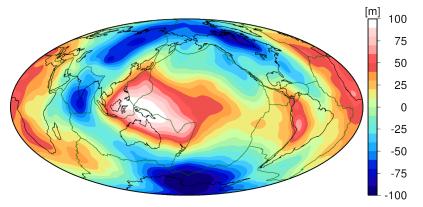


Geoid anomalies

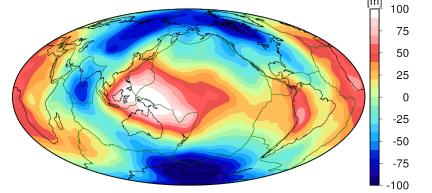


*I*_{max} = 180 – Nakiboglu (1982) non-hydrostatic

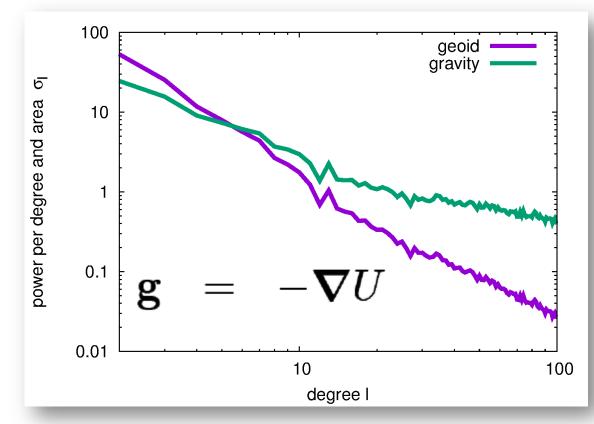
 $I_{\text{max}} = 31 - \text{Nakiboglu} (1982) \text{ non-hydrostatic}$



 $I_{\text{max}} = 31 - \text{Chambat et al.}$ (2010) non-hydrostatic



Potential field constraints: Bias in wavelength dependence of model fit

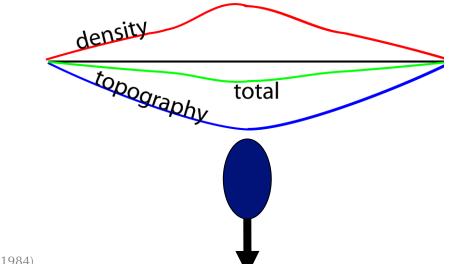


Let's fit the geoid: Static effect of dense anomaly

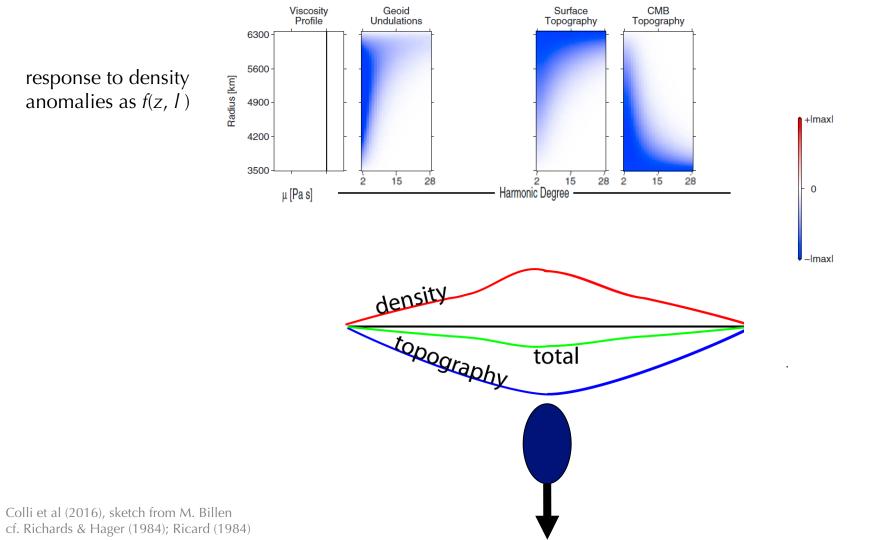


sketch from M. Billen's MYRES talk cf. Hager (1984); Richards & Hager (1984); Ricard (1984)

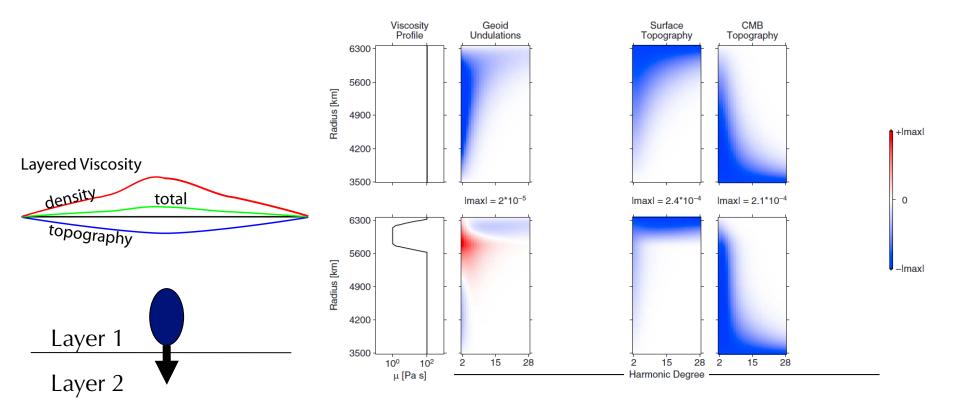
Combined static and dynamic effect of a slablet



sketch from M. Billen's MYRES talk cf. Hager (1984); Richards & Hager (1984); Ricard (1984)



Kernels for layered viscosity mantle

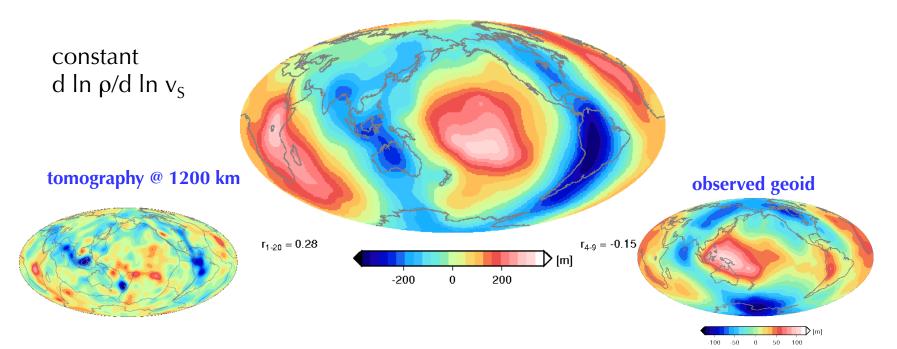


Colli et al (2016), sketch from M. Billen; cf. Richards & Hager (1984); Ricard (1984)

Geoid for tomography driven flow

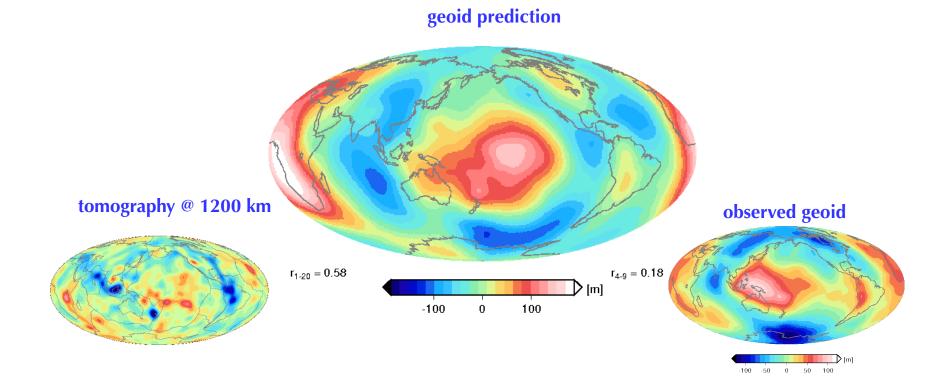
• Isoviscous – free slip surface boundary condition

geoid prediction



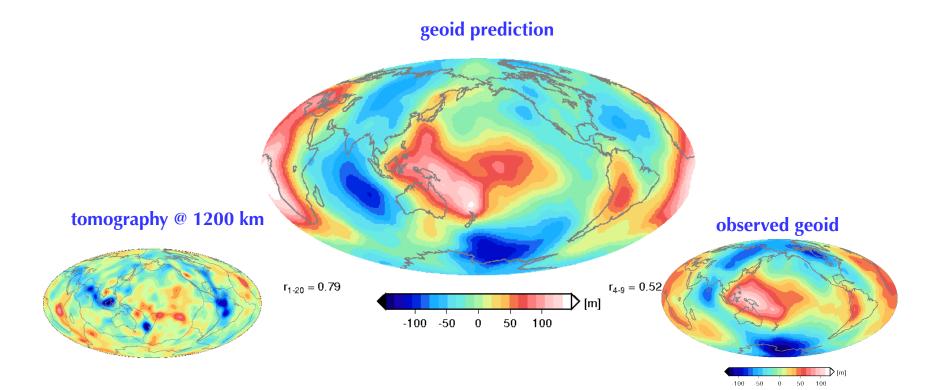
Geoid for tomography driven flow

• Lower mantle viscosity increase

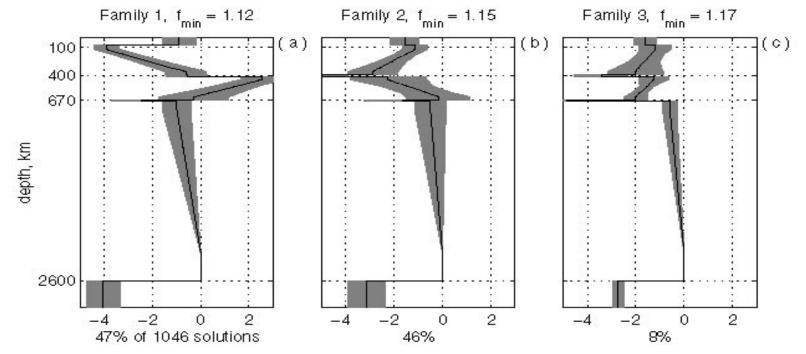


Geoid for tomography driven flow

• Four layer model



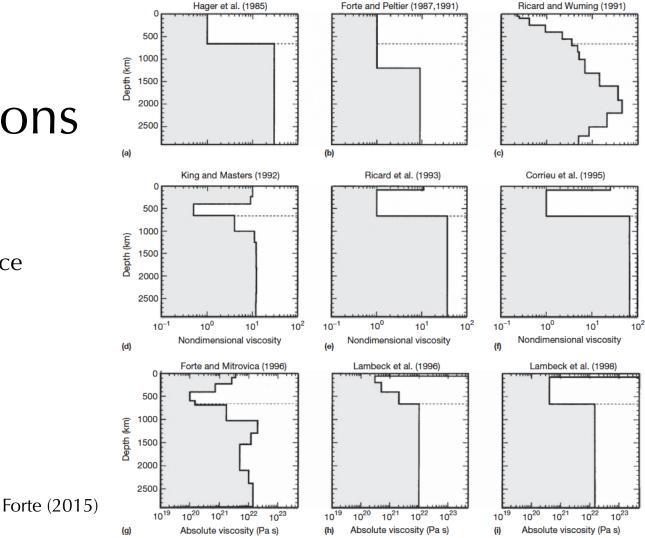
Viscosity inversions are non-unique (Monte Carlo approach, based on geoid and surface dynamic topography)



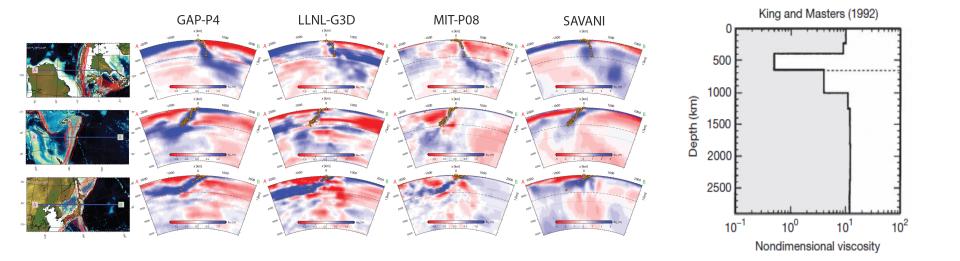
Panasyuk & Hager (2000)

Geoid vs. GIA inversions

still need to reconcile ice load model viscosities

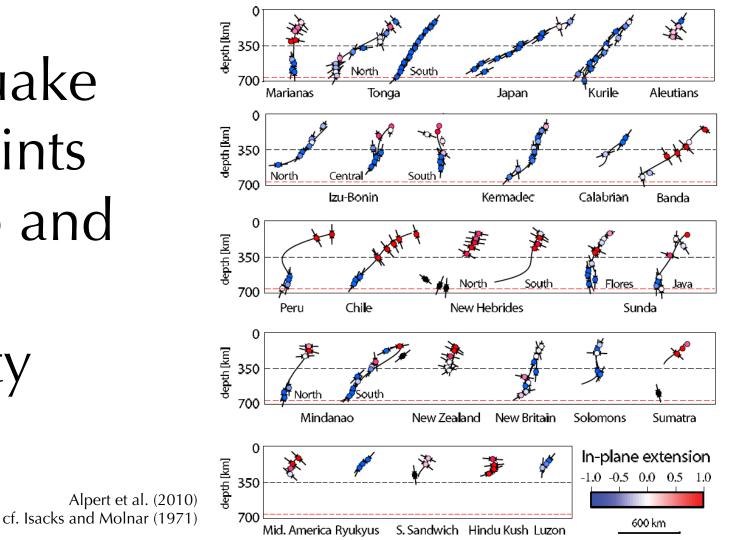


Slab ponding diversity and viscosity stratification in transition zone

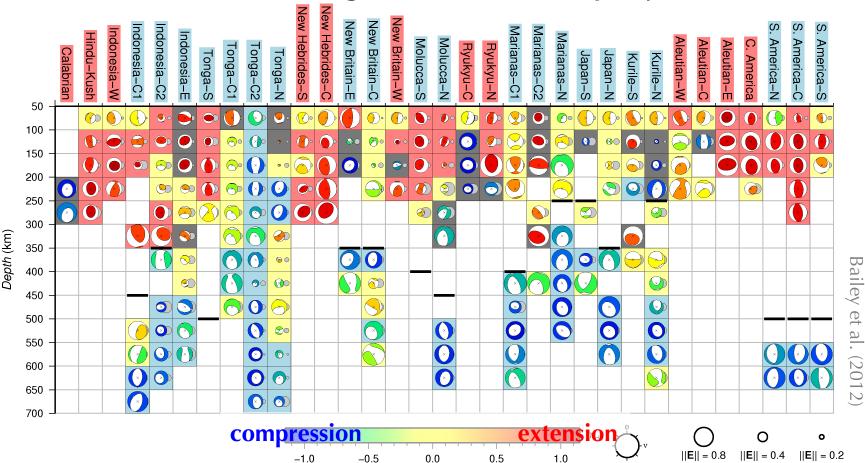


cf. Fukao and Obayashi (2013) King and Masters (1992) Rudolph et al. (2016)

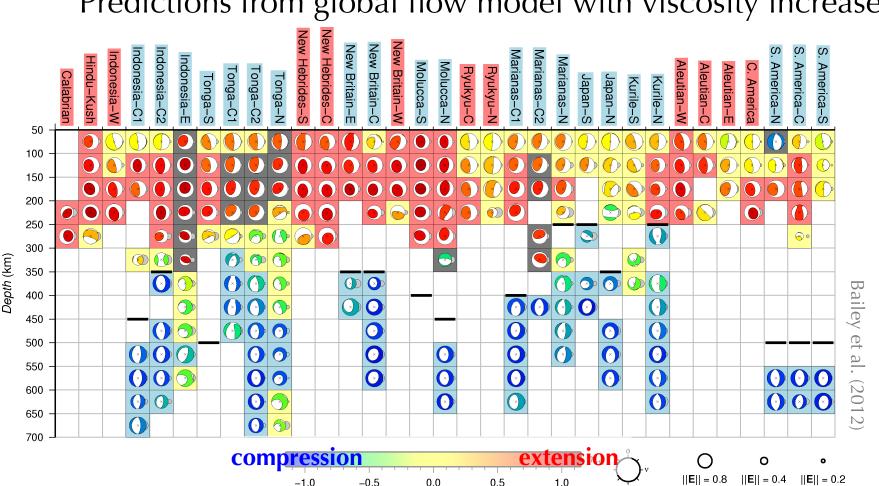
Earthquake constraints for slab and mantle viscosity



Summed gCMTs (in-slab projection)

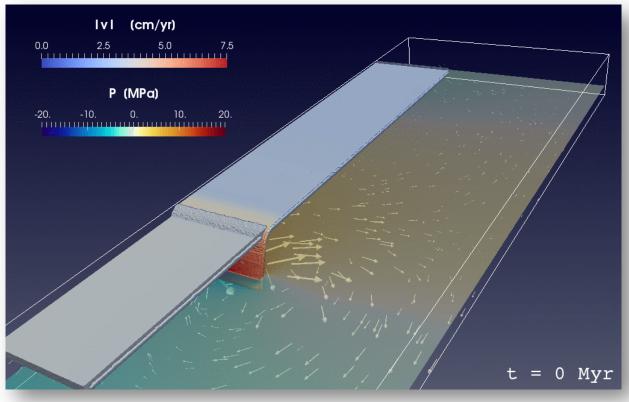


Alisic cf. Vassiliou and Hager (1998), et al. (2010),Alpert et al Billen and (2010)Gurnis (2003)



Predictions from global flow model with viscosity increase

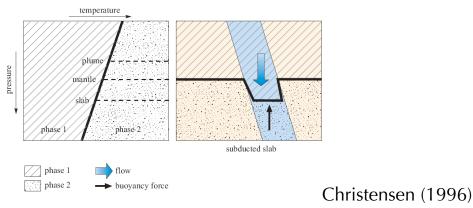
Regional subduction dynamics (let's do our own experiments)

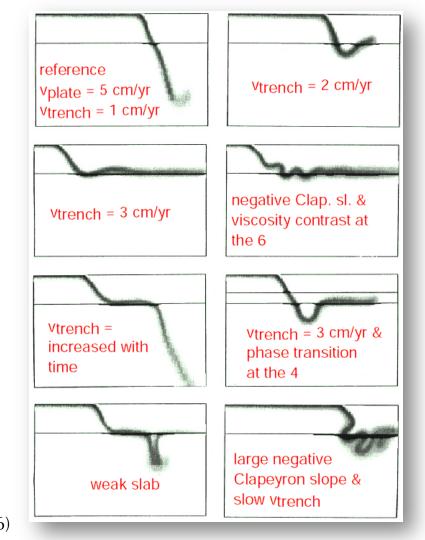


Holt et al. (2017)

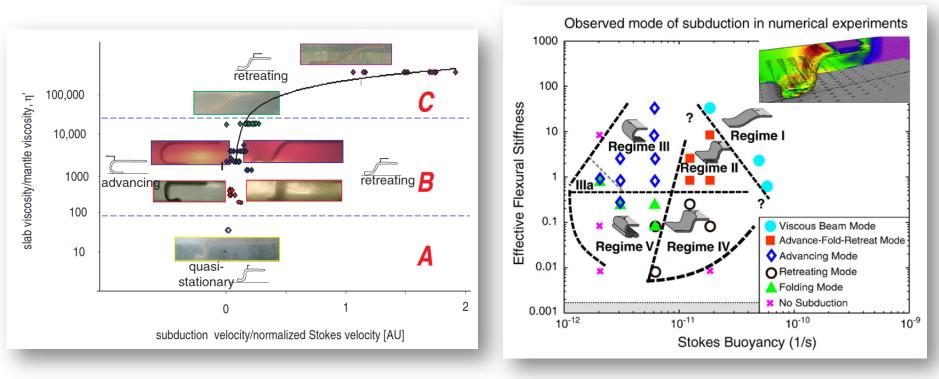
Trench rollback and slab penetration

- kinematic (prescribed velocities) model varying plate/trench motion partitioning and importance of phase transition (v_{trench} vs. v_{Stokes})
- Δρ due to deeper phase transition for negative Clapeyron slope





Rollback dynamics phase diagrams

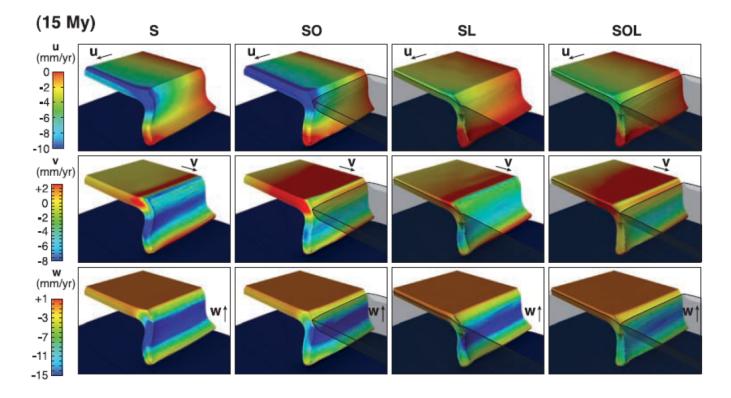


Stegman et al. (2010)

Funiciello et al. (2007)

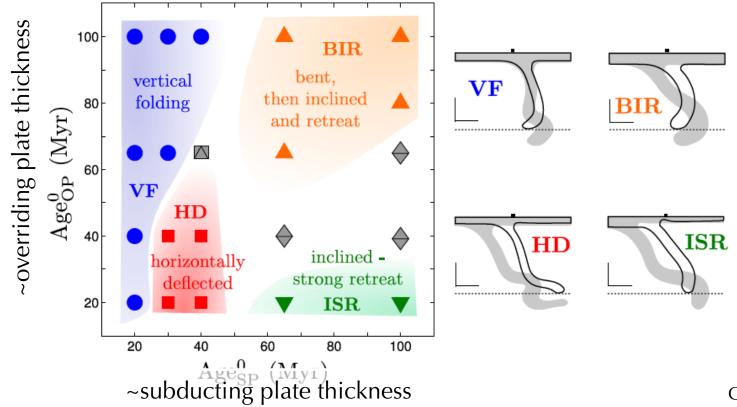
cf. Ribe (2010)

Annoyances I: The overriding plate



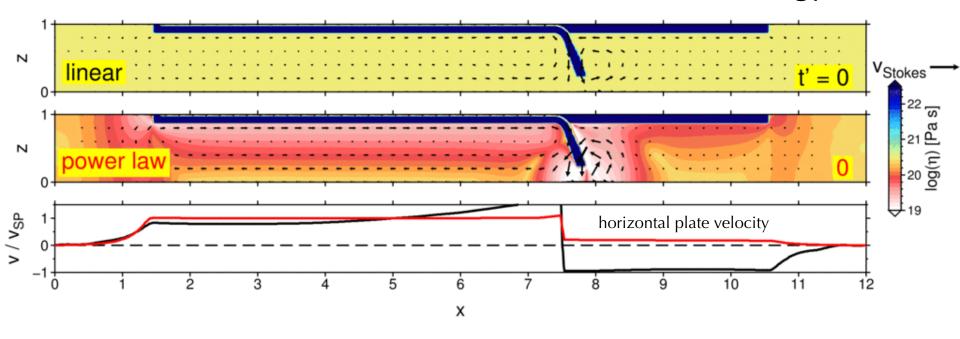
Yamato et al. (2009)

New regime diagrams for trench motions and ponding



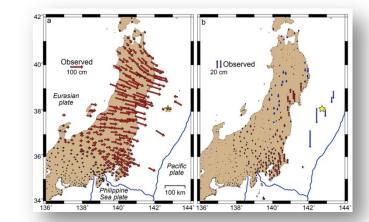
Garel et al. (2014)

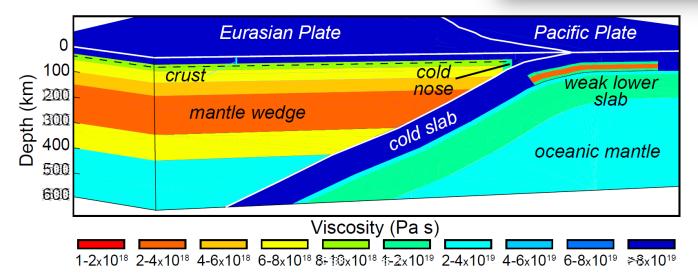
Annoyance II: Trench motions for nonlinear mantle rheology



Holt and Becker (2017); cf. Billen and Hirth (2003), Jadamec and Billen (2012)

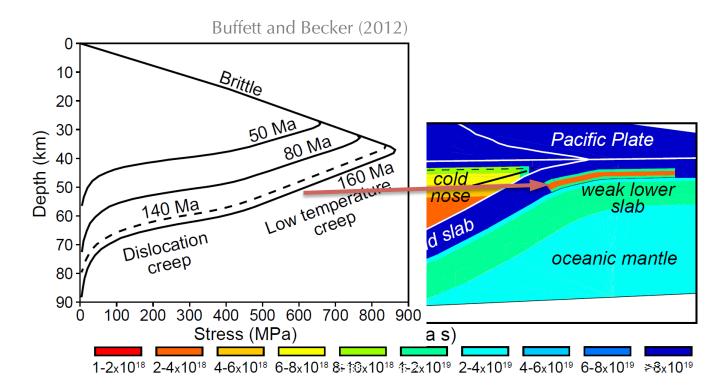
Large-scale rock mechanics experiment: Infer slab and mantle rheology from post-seismics (Tohoku-oki 2011 M9)





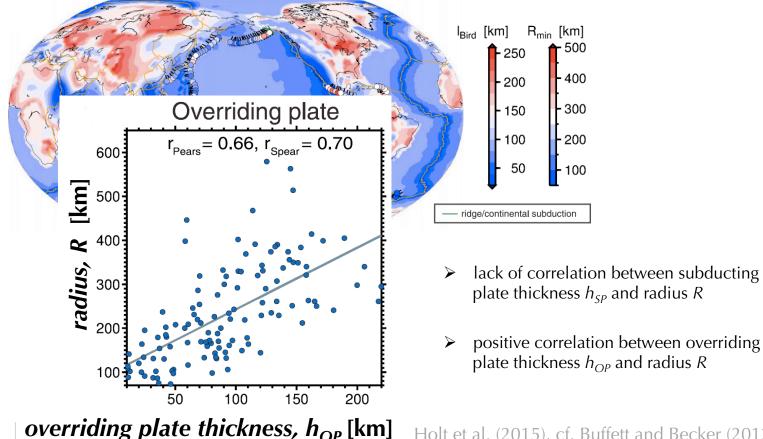
Freed et al. (2016), cf. Wu et al. (2015)

Plastic slab I: Weakening of oceanic plate by Peierls creep?



Freed et al. (2016)

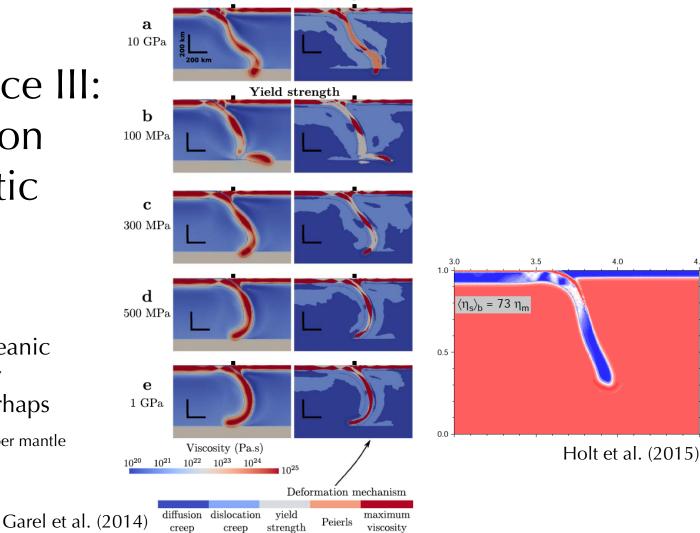
Plastic slab II: Overriding plate thickness controls bending radius for plastic, not for viscous plate – Earth behaves like that



Holt et al. (2015), cf. Buffett and Becker (2012)

Annoyance III: **Subduction** withplastic rheology

➤ significant oceanic plate viscosity reduction, perhaps $\eta_{slab}{\sim}100~\eta_{upper~mantle}$

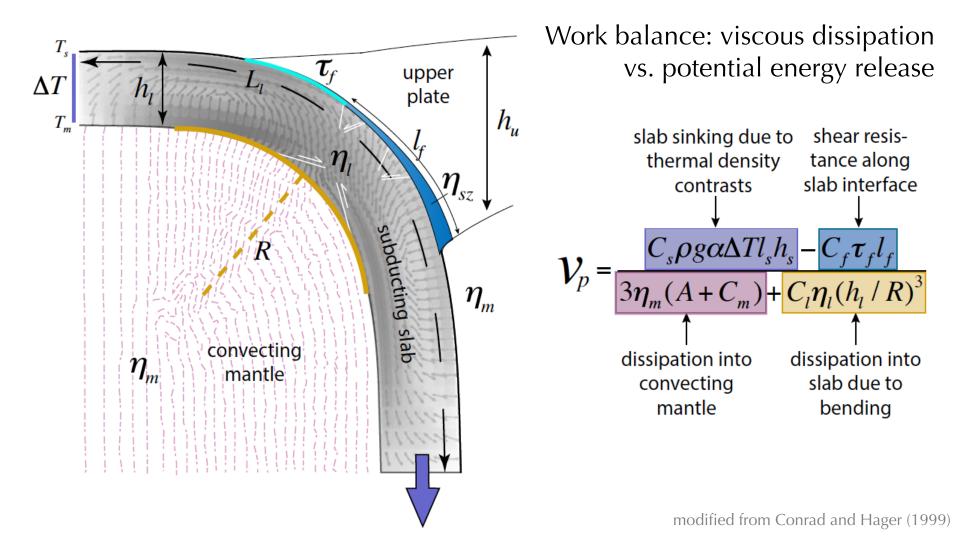


4.5

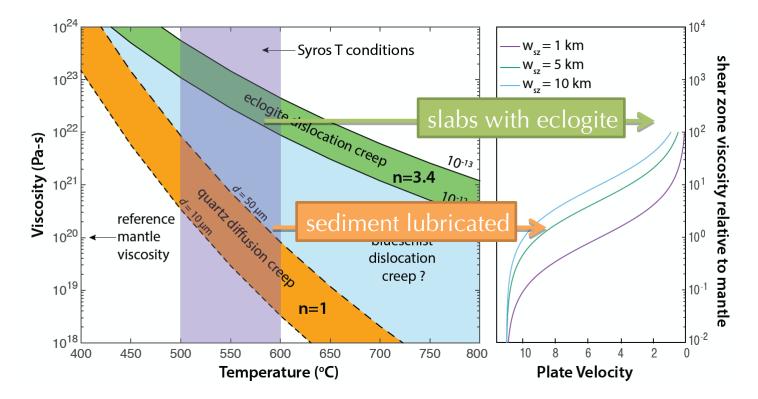
log₁₀(η/10²¹Pas)

0

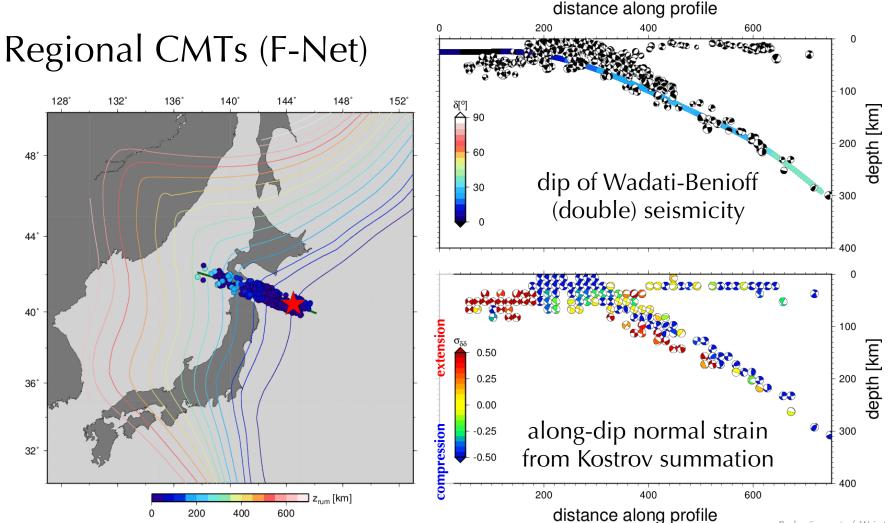
- -1



Annoyance IV: Interface (i.e. geology) control on plate velocities (continental erosion, long term cycles)?

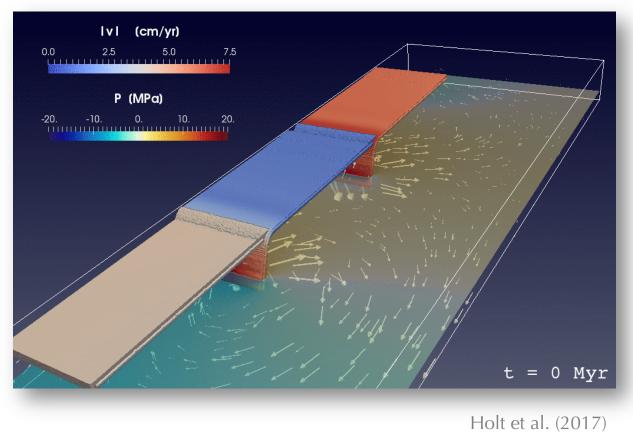


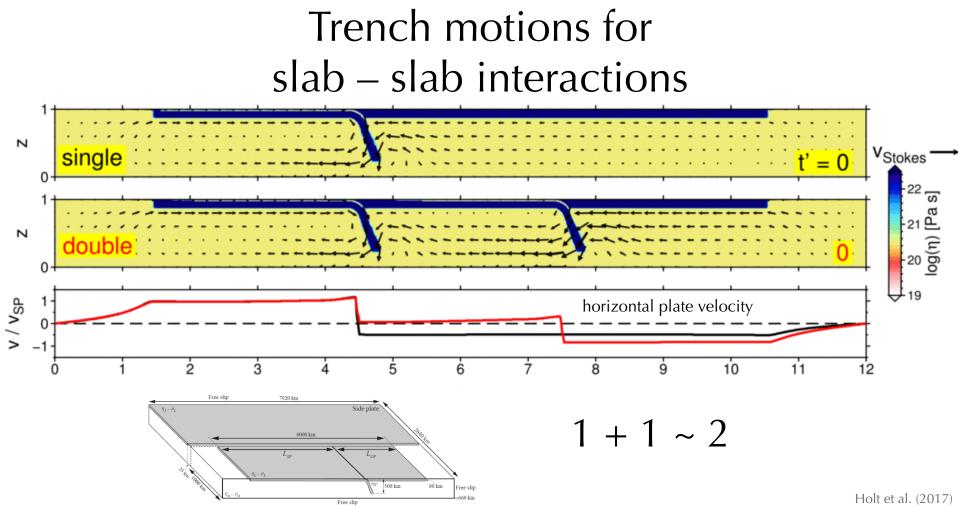
Behr and Becker (in prep.), cf. Buffett and Becker (2012)



Becker (in prep), cf. Wei et el. (2017)

Slab – slab interactions



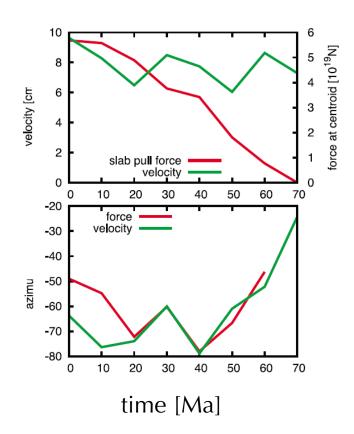


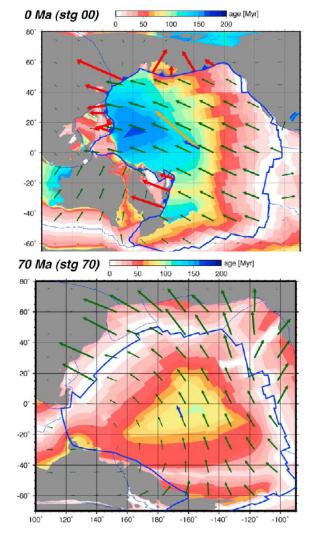
cf. Cizcova and Bina (2015); Jagoutz et al. (2015); Faccenna et al. (submitted)

130 150 Global interactions: Trench motions and reference frames rollback GJ86 n° of subduction zones advance Mean 9.33 Standard error 2.23 Median 8.68 σ 29.22 Min -63.4 Max 123.1 σ Min Max v_T [mm/yr] 40 0 30 60 90 120 150 Becker et al. (2015) 5.0 Myr advancing retreatir V_{t(n)} (mm/yr) Funiciello et al. (2008) Zhong and Gurnis (1995) Gerault et al. (2011)

120 50° |

Upper mantle slabs are not the whole story...

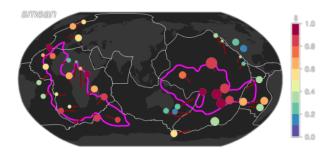




Faccenna et al. (2011) cf. Gordon

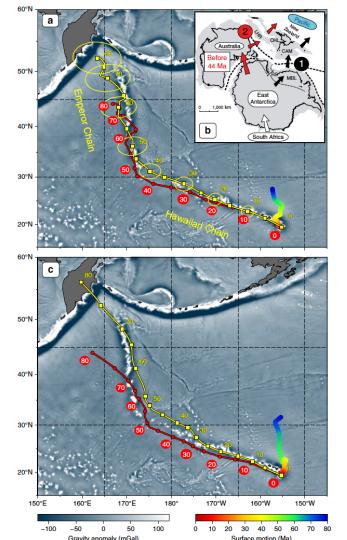
How about plumes?

- Did the plumes or the plates move to cause hotspot track bends?
- Can we predict plume conduits?



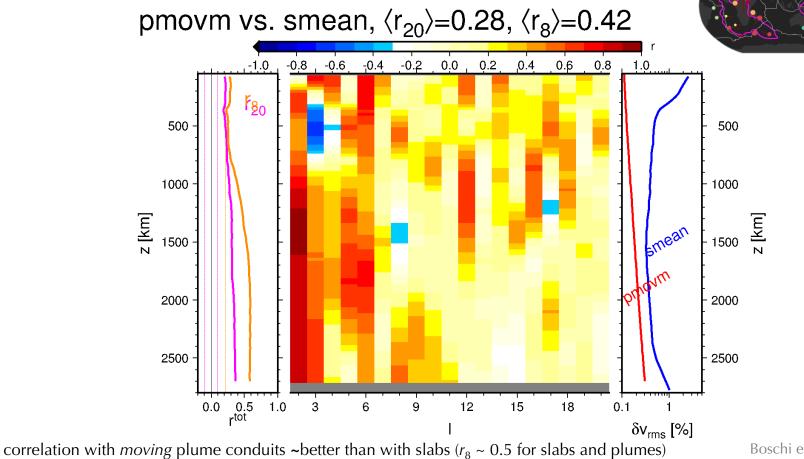
Torsvik et al. (2017)

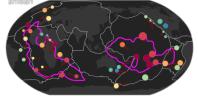
cf. Steinberger (2000); Tarduno et al. (2009); Hassan et al. (2016)



Advected plumes vs. tomography

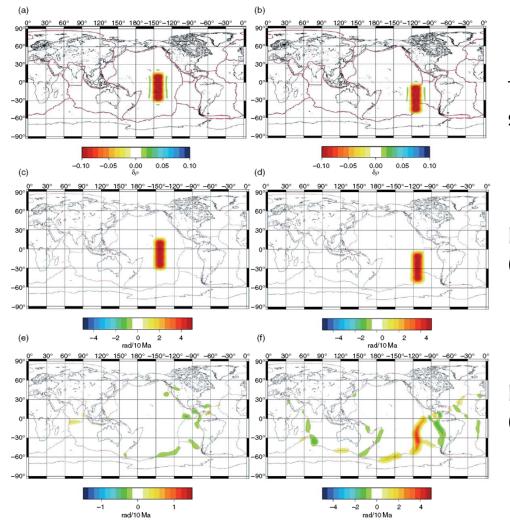
 \geq





Boschi et al. (2007, 2008)

Plumes as plate driving forces



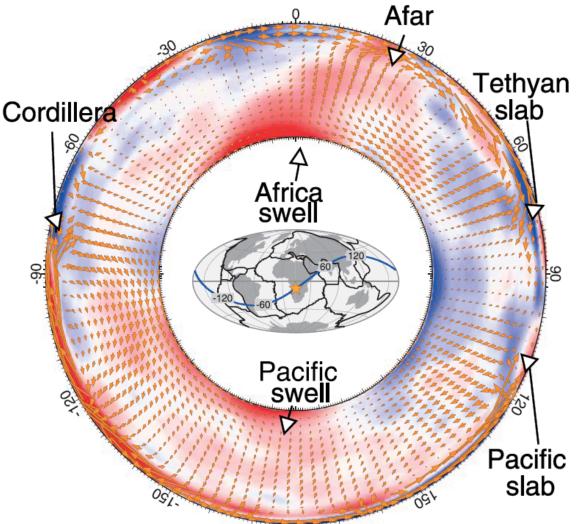
Two density sources

Free-slip solution (poloidal only)

Plate solution (poloidal only)

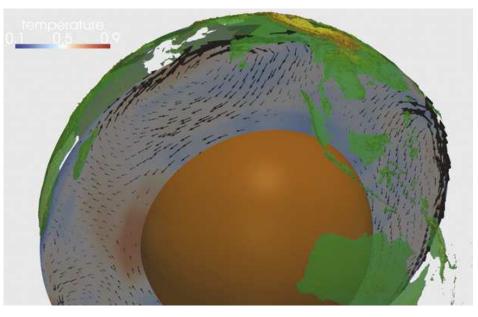
Forte (2015)

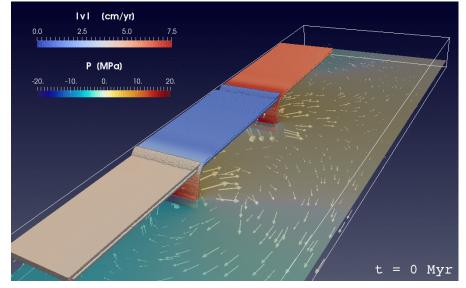
Mantle conveyor belts



Faccenna et al. (2013)

India's motion at present: Mantle conveyor belt, broad-scale upwelling push?

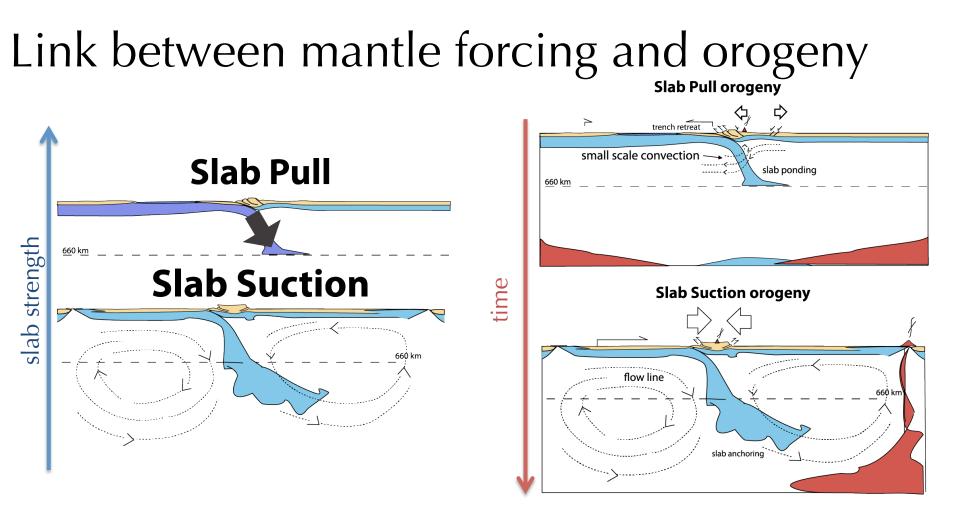




Jagoutz et al. (2015); Holt et al. (2017)

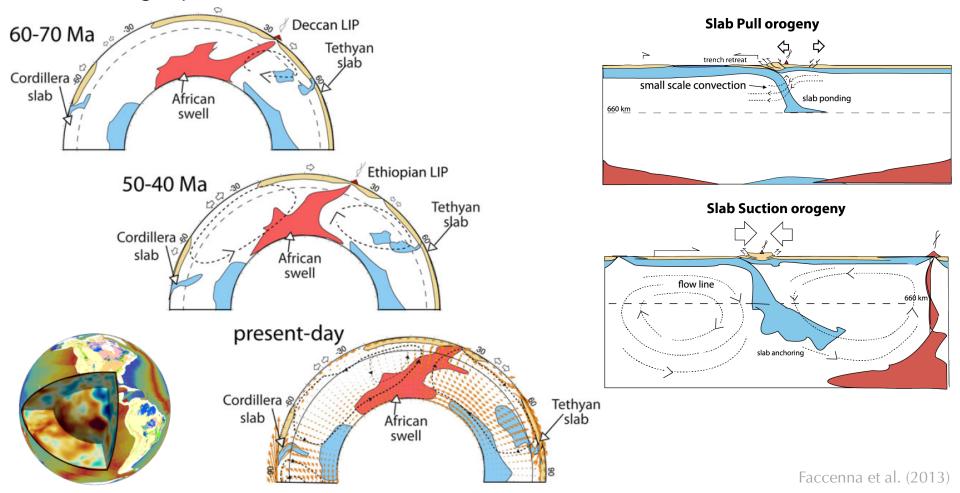
India's motion in the past: Double slab dynamics?

Becker and Faccenna (2011)

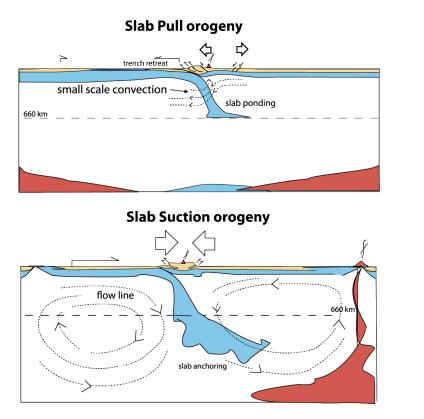


Faccenna et al. (2013); Yamato et al. (2013)

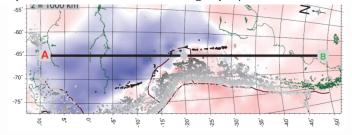
Tibetan orogeny linked to establishment of whole mantle convection cell

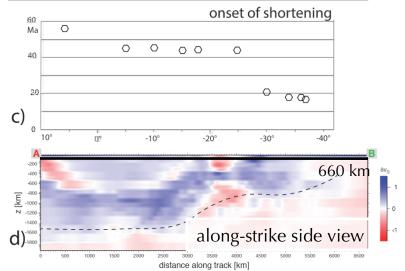


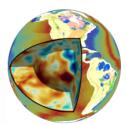
Subduction and orogeny: links between convection and continental geology (Andes)



map view of seismic tomography under Andes



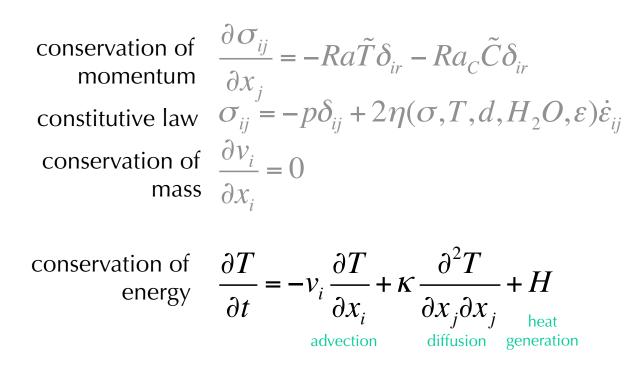




Faccenna et al. (2017)

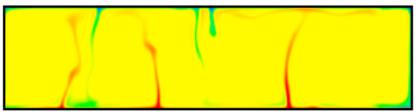
Mantle convection

- > energy equation governs planetary heat loss
- > introduces time-dependence and non-linearity (coupling between velocity and temperature)
- > can time reverse advection, but not diffusion

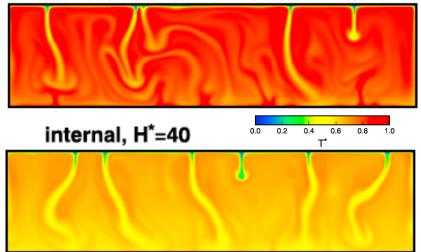


Slabs are part of heat transport – effect of heating mode isoviscous fluid

basal

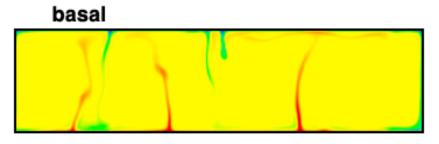


mixed, H*=40

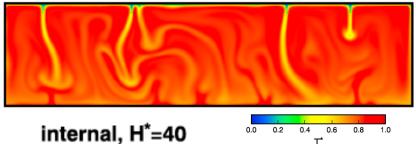


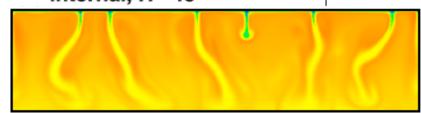
Korenaga (2017)

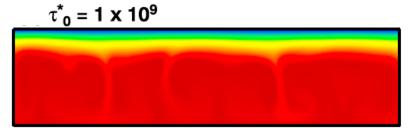
Slabs are part of heat transport – effect of heating and plate mode isoviscous $\eta(T)$ + yielding (mixed heating)



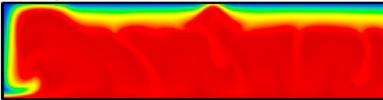
mixed, H*=40



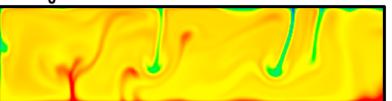




 $\tau_0^* = 2 \times 10^5$

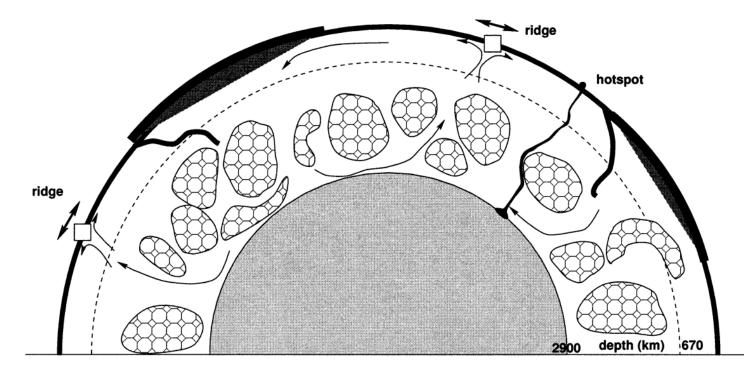


 $\tau_0^* = 2 \times 10^4$



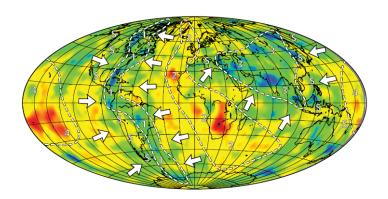
Korenaga (2017), cf. Foley and Becker (2009)

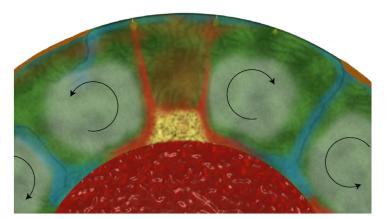
The role of viscous blobs and other (e.g. LPO induced) mechanical anisotropy for convective stability

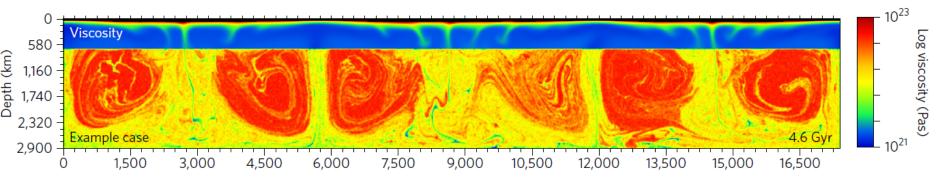


Becker et al. (1999), cf. Manga (1996)

BEAMs stabilizing conveyor belts?

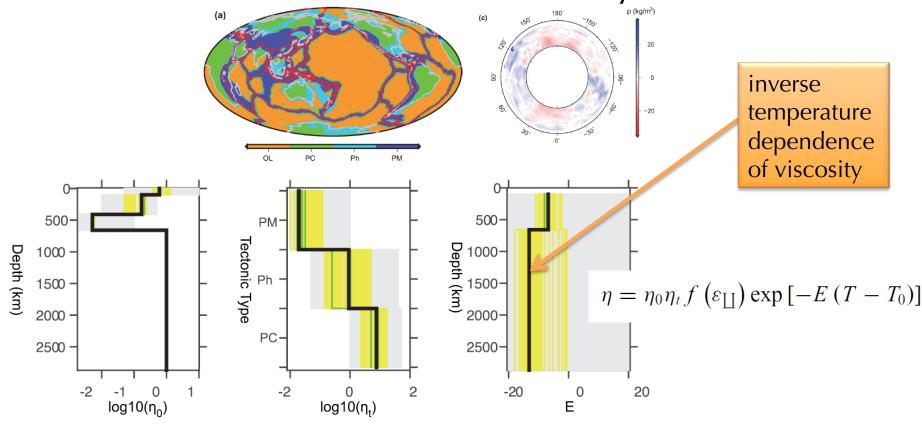






Ballmer et al. (2017)

Inversions for lateral viscosity variations



Yang and Gurnis (2016)

Conclusions

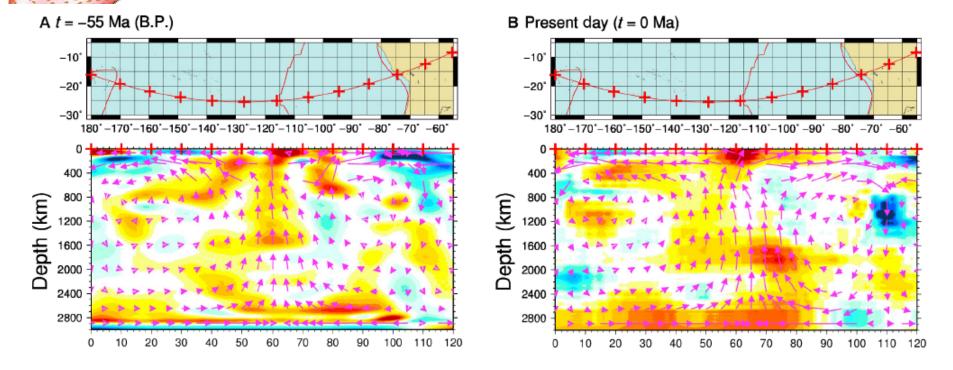
subduction controls tectonics (including orogeny) and heat loss (by setting mantle convection's spatio-temporal scales)

 \diamond subduction interface may affect plate velocities in a weak slab world

- potential links between continental dynamics and deep mantle may help decipher planetary evolution
- make progress by integrating diverse datasets in inverse models, e.g. to better constrain mantle and slab rheology
- use tools that capture global, multi-scale interactions of mantle flow for regionally realistic subduction models

Additional slides

Persistence of upwellings?

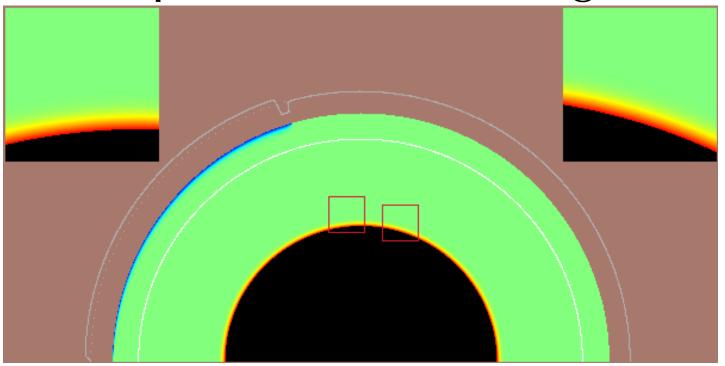


➤ active upwelling underneath East Pacific Rise since 50 Ma?

120

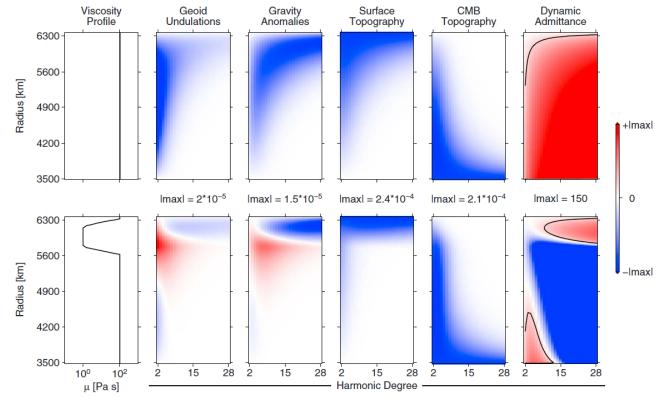
Rowley et al. (2016)

Ying and yang of up and downwellings

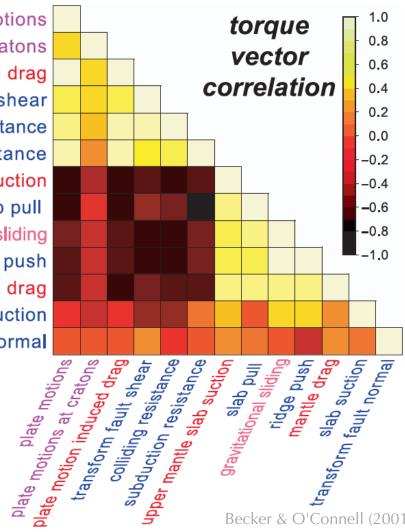


Tan et al. (2001)

Kernels for layered viscosity mantle



Colli et al (2016) cf. Hager & Richards (1984); Ricard (1984)



Becker & O'Connell (2001)

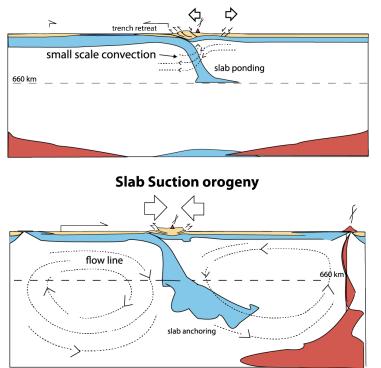
plate motions plate motions at cratons plate motion induced drag transform fault shear colliding resistance subduction resistance upper mantle slab suction slab pull gravitational sliding ridge push mantle drag slab suction transform fault normal

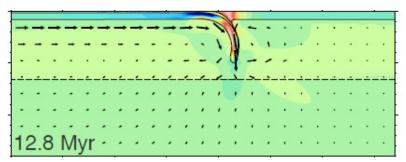
edge forces

mantle tractions

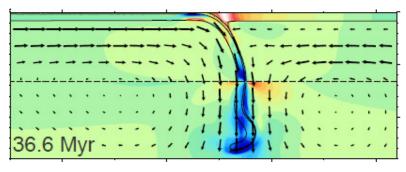
Time-dependent compressional stresses during subduction penetration related to onset of crustal shortening?

Slab Pull orogeny



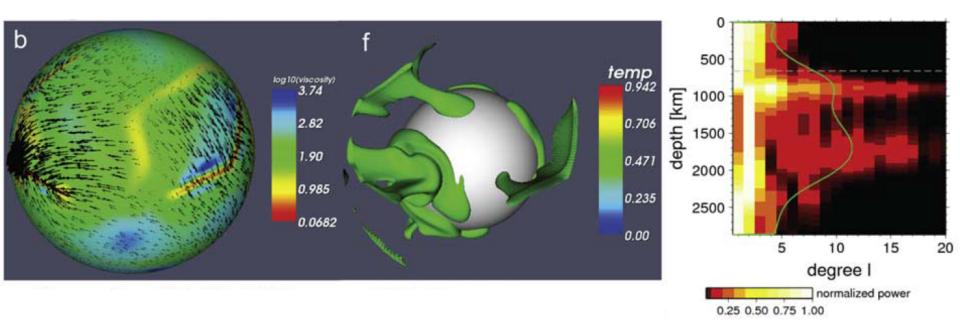


red = horizontal compression
blue = horizontal extension

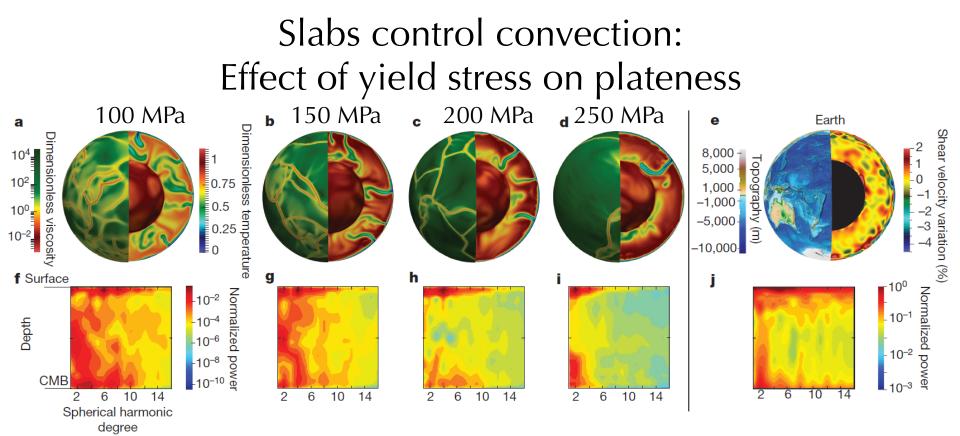


cf. Machetel and Weber (1991); Tackley et al. (1993); Pysklywec and Mitrovica (1997)

How are the plates made? $\eta(T) \& \tau_{\text{yield}}, \eta(z)/f_{\text{melt}} \Delta \rho_{c'} \eta(\phi)$



Foley and Becker (2009)

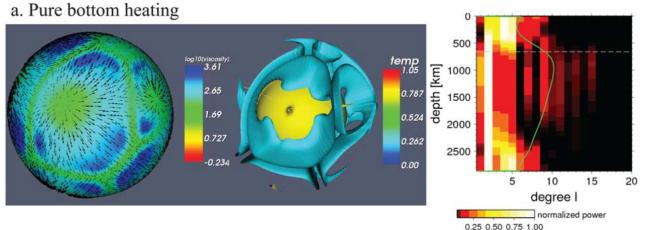


Mallard et al. (2016)

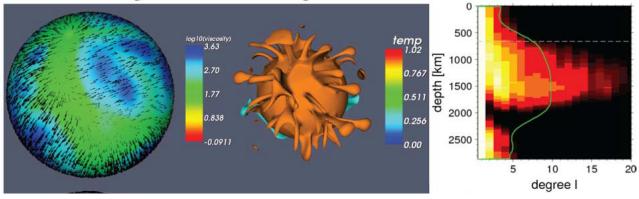
cf. Tackley (2000a,b), Richards et al. (2001), van Heck and Tackley (2008), Foley and Becker (2009)

But: effect of asthenosphere, internal vs. bottom heating, Ra #, continents, and damage/memory

Plumes breaking plates



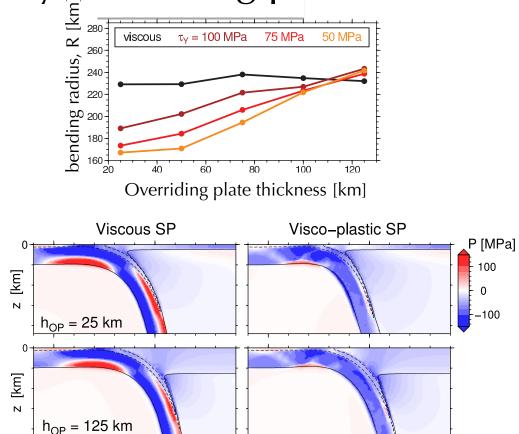
b. Bottom heating, 60 % internal heating



Foley and Becker (2009)

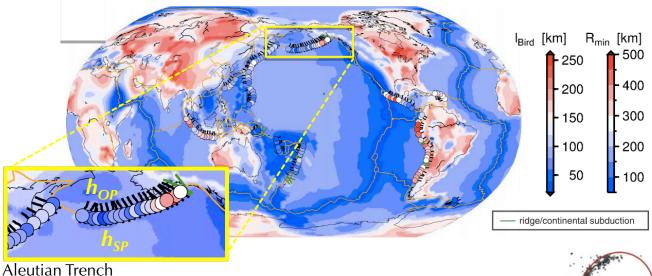
Effectively plastic slab: Bending radius affected by overriding plate thickness

Plastic slab more strongly affected by lifting force $(F_{\Delta P})$ associated with overriding plate, weak bending stresses

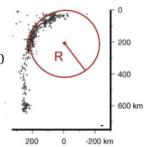


Holt et al. (2015)

Bending radius and plate thickness in nature

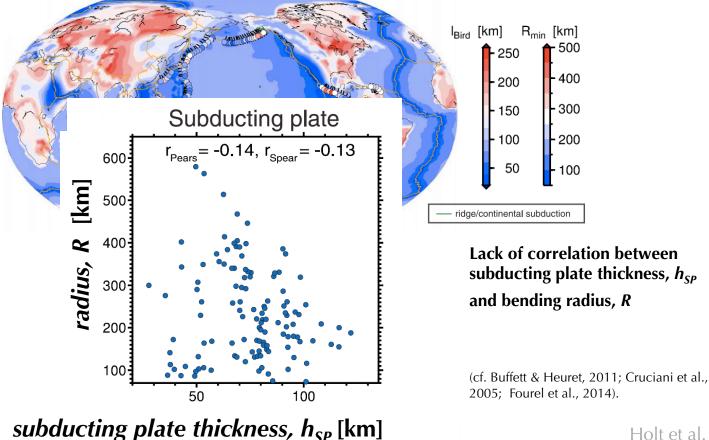


- Radii of curvature from Benioff zone spline fits (Buffett & Heuret, 20
- Lithospheric thickness estimated from seismic tomography and seafloor age (Bird et al., 2008)



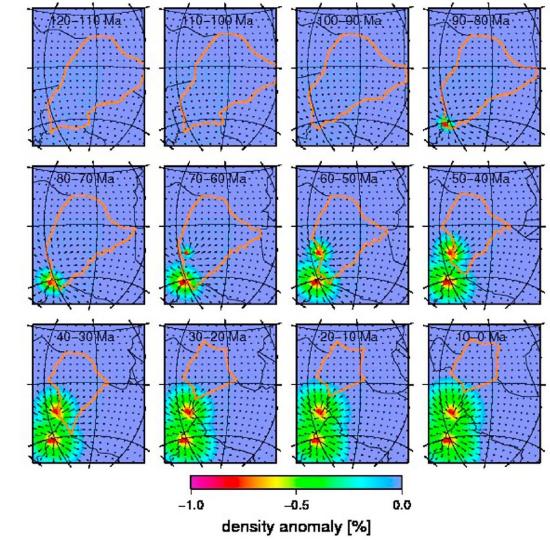
Holt et al. (2015)

No subducting plate control on slab curvature



Holt et al. (2015)

Plate driving forces: plumes



van Hinsbergen et al. (2011)

